



Facile Synthesis of Single Phase Pr-Doped BiFeO₃ Nanoparticles via a Sol-Gel Auto Combustion Technique

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Received: 13 February 2025;

Accepted: 19 March 2025;

Published online: 29 March 2025;

AJC-21953

In this study, the synthesis of single-phase Pr-doped bismuth ferrite, Bi_{1-x}Pr_xFeO₃ ($x = 0, 0.05, 0.07$ and 0.10) nanoparticles by the sol-gel auto-combustion method, followed by calcination at $400\text{ }^{\circ}\text{C}$, is reported. Thermogravimetric analysis (TGA), Fourier transform infrared spectroscopy (FT-IR), transmission electron microscopy (TEM) and X-ray diffraction (XRD) techniques were used to characterize the samples. TEM images illustrate the formation nearly spherical nanoparticles in the size range of $30\text{--}80\text{ nm}$. XRD confirmed the formation of single phase and well-crystallized Bi_{1-x}Pr_xFeO₃ nanoparticles at $400\text{ }^{\circ}\text{C}$. XRD results show a gradual shift and merge of diffraction peaks on increasing doping concentration of Pr³⁺ in the BiFeO₃ matrix, which suggested a structural phase transition.

Keywords: Bismuth ferrite, Sol-gel, Autocombustion, Nanoparticles.

INTRODUCTION

The interest in perovskite bismuth ferrite (BiFeO₃) has increased in recent years due to its exceptional physical properties, including a notably high Curie temperature ($T_C \approx 1100\text{ K}$) as well as Néel temperature $T_N \approx 643\text{ K}$ [1]. These characteristics make BiFeO₃ an excellent candidate for room temperature multiferroic materials, which have promising applications in fields of spintronic devices [2,3]. Beyond its multiferroic properties, BiFeO₃ has also emerged as a potential visible-light-driven photocatalyst for the degradation of organic dye due to its small band gap ($\sim 2.0\text{--}2.5\text{ eV}$) [4]. The small band gap, chemical stability and intrinsic electric polarization field of BiFeO₃ provide a foundation for photocatalytic activity under visible light [4-6]. Despite these advantages, the practical application of BiFeO₃ in photocatalysis remains limited due to the rapid recombination of photogenerated electron-hole pairs, which significantly reduces its photocatalytic efficiency [7]. Therefore, it is an interesting task to improve the photocatalytic activity of BiFeO₃ for practical use.

To achieve this purpose there are many innovative strategies that are used to overcome the limitations of rapid electron-hole recombination in BiFeO₃ and enhance its photocatalytic

performance. Some of these approaches are as follows: creating nanoscale morphologies of BiFeO₃ to increase its surface area and provide more active sites for photocatalytic reactions. Introducing suitable dopants into the BiFeO₃ lattice to reform its electronic structure, enhance light absorption and suppress electron-hole recombination, forming heterojunctions with complementary semiconductors to facilitate efficient charge transfer and separation and modifying the surface properties to improve adsorption of reactants and stabilize charge carriers [8-11]. Recently, it has been investigated that among the above approaches, the doping at either the Bi or Fe site of the BiFeO₃ lattice plays a crucial role in altering its properties. In this regard, rare earth element doping has gained significant attention in modifying the properties of BiFeO₃. Rare earth dopants can act as trapping sites for electrons or holes, promoting the separation and efficient production of photogenerated charge carriers during photocatalytic reactions and increasing photocatalytic properties [12,13].

Doping with foreign atoms, such as dysprosium, gadolinium or manganese, at the Bi or Fe sites of the BiFeO₃ lattice has demonstrated notable improvements in photocatalytic activity [14-16]. For instance, Sakar *et al.* [14] reported that substituting Bi³⁺ with Dy³⁺ in BiFeO₃ resulted in a significant

enhancement in photocatalytic performance under visible light irradiation. Zhang *et al.* [16] reported that the photocatalytic activity of BiFeO₃ was enhanced by the doping of Gd. Despite these advancements, research on rare earth doping in BiFeO₃ for photocatalytic applications is still in its infancy, with numerous challenges remaining.

In many challenges, one big challenge is the preparation of phase pure and doped bismuth ferrite nanoparticles. BiFeO₃ is stable at a very narrow temperature range, hence, it is challenging to synthesize it with controlled structural features and high surface area [5,17]. To date, a number of techniques have been tried to synthesize nanosized BiFeO₃ such as solid-state reaction, co-precipitation, sonochemical, solution combustion and sol-gel process [18,19]. However, there are some drawbacks to these methods as they are either complex or require high calcination temperatures. Due to high calcination temperature, bismuth is lost due to volatilization, which results in the formation of impurity phases like Bi₂Fe₄O₉, Bi₃₆Fe₂₄O₅₇, Bi₂O₃, *etc.* along with the formation of BiFeO₃ phase [20]. Among these, the sol-gel approach has an advantage over other methods because the material synthesized by this method has a good surface area, good homogeneity and precise control over stoichiometry.

In this method, different types of complexing agents have been used to synthesize BiFeO₃ nanoparticles. For example, Park *et al.* [21] synthesized BiFeO₃ nanopowder of different particle sizes using ethylene glycol as a complexing agent. Liu *et al.* [22,23] used polyvinyl alcohol and glycerol as complexing agents to synthesize pure BiFeO₃ phase at 400 °C. Similarly, Ghosh *et al.* [24] synthesized phase pure BiFeO₃ powder using tartaric acid as a complexing agent. Further, it is observed that when a weaker complexing agent is replaced by a stronger complexing agent (EDTA, succinic acid) phase pure BiFeO₃ is not formed [20]. Therefore, it is reasonable to speculate that a weaker complexing agent may be utilized for the synthesis of phase pure BiFeO₃.

Future studies are needed to optimize doping strategies and investigate the relation between the dopant concentration, structural changes and property alteration in order to fully utilize the potential of doped BiFeO₃. Keeping all the above perspectives in mind, in this work, we synthesized phase pure BiFeO₃ and 5%, 7% and 10% Pr-doped BiFeO₃ nanoparticles using a facile sol-gel autocombustion method using propylene glycol as a complexing agent, followed by calcination at 400 °C. The crystal structure and morphologies were also investigated.

EXPERIMENTAL

Analytical grade bismuth nitrate pentahydrate (Bi(NO₃)₃·5H₂O, 99.99%), ferric nitrate nonahydrate (Fe(NO₃)₃·9H₂O, 99.95%) and praseodymium nitrate hexahydrate (Pr(NO₃)₃·6H₂O, 99.9%) were procured from Sigma-Aldrich, USA. Nitric acid (69%) was procured from Merck and propylene glycol (C₃H₈O₂) was supplied from Thermofisher. For the preparation of bismuth ferrite nanoparticles, 3 mmol of bismuth nitrate pentahydrate was dissolved in 50 mL of dilute nitric acid. Similarly, 3 mmol of ferric nitrate nonahydrate was dissolved in 50 mL of distilled water in a separate beaker. Both solutions

were then mixed to form 100 mL precursor solution, which was kept on a magnetic stirrer for heating and stirring. During continuous heating, 1 mL of propylene glycol was added as a complexing agent. The mixture was then heated between 100-120 °C while being continuously stirred to remove any excess water. As water evaporates and the viscosity of the solution increases, gel formation occurs. Subsequently, after auto combustion a brown powder was obtained. The brown powder was then scratched out from the beaker and ground into a fine powder to obtain the BiFeO₃ precursor powder. Finally, this precursor powder was calcined at 400 °C for 2 h in a muffle furnace to obtain well-crystallized BiFeO₃ nanoparticles.

Further, for the synthesis of 5%, 7% and 10% Pr-doped bismuth ferrite nanoparticles Bi_{1-x}Pr_xFeO₃ (*x* = 0.05, 0.07 and 0.10), bismuth nitrate pentahydrate, ferric nitrate nonahydrate and praseodymium nitrate are used in stoichiometric proportions. For example, to synthesize 3 mmol of Bi_{0.95}Pr_{0.05}FeO₃, 1.382 g of bismuth nitrate was dissolved into dil. nitric acid solution, 1.212 g of ferric nitrate and 0.065 g of praseodymium nitrate were dissolved in distilled water. Once all metal nitrate solutions were prepared and then combined to form a precursor solution followed by the addition of 1 mL of propylene glycol. This mixture was stirred continuously at 100-120 °C until all the liquid evaporates, forming a gel-like fluid. As the process continues, the gel transforms into a fluffy precursor powder. Finally, this precursor powder undergoes calcination in a muffle furnace at 400 °C for 2 h. This step ensures the formation of well-crystallized Bi_{0.95}Pr_{0.05}FeO₃ nanoparticles, which can then be characterized and used for further applications. Similarly, we synthesized Bi_{0.93}Pr_{0.07}FeO₃ and Bi_{0.90}Pr_{0.10}FeO₃.

Characterization: The precursors were subjected to thermogravimetric analysis (TGA) using a Mettler Toledo Star System TGA apparatus up to 850 °C under ambient atmospheric conditions. Fourier transform infrared (FT-IR) spectra were recorded in the range of 400-4000 cm⁻¹ using Bruker Vertex 70. X-ray diffraction (XRD) studies were carried out using X'Pert Pro, PANalytical over a 2θ range of 20° to 60°. Transmission electron microscopy (TEM) studies were carried out using FEI Technai G² U-Twin.

RESULTS AND DISCUSSION

TGA analysis: Fig. 1 shows the thermal decomposition of the BiFeO₃ and Bi_{0.90}Pr_{0.10}FeO₃ precursor powder. The TGA curve displays several stages of decomposition of the complex which is most likely formed during the reaction, such as the loss of carbonized, non-carbonized and water molecules and it shows an overall weight loss of 41% and 43% for BiFeO₃ and Bi_{0.90}Pr_{0.10}FeO₃ precursor, respectively. There is no noticeable weight loss beyond 400 °C which suggests the phase formation temperature of pure and Pr-doped BiFeO₃ is 400 °C.

FT-IR analysis: Fig. 2 shows the FT-IR spectra of pure and Pr-doped BiFeO₃ nanoparticles calcined at 400 °C for 2 h. The band near 3400 cm⁻¹ in all samples is assigned to anti-symmetric stretching in O-H from adsorbed water due to the contact of the samples with the environment. The bands at about 548 cm⁻¹ and 445 cm⁻¹ in BiFeO₃ can be assigned, respectively, to the mode ν of stretching vibrations along the Fe-O axis, to

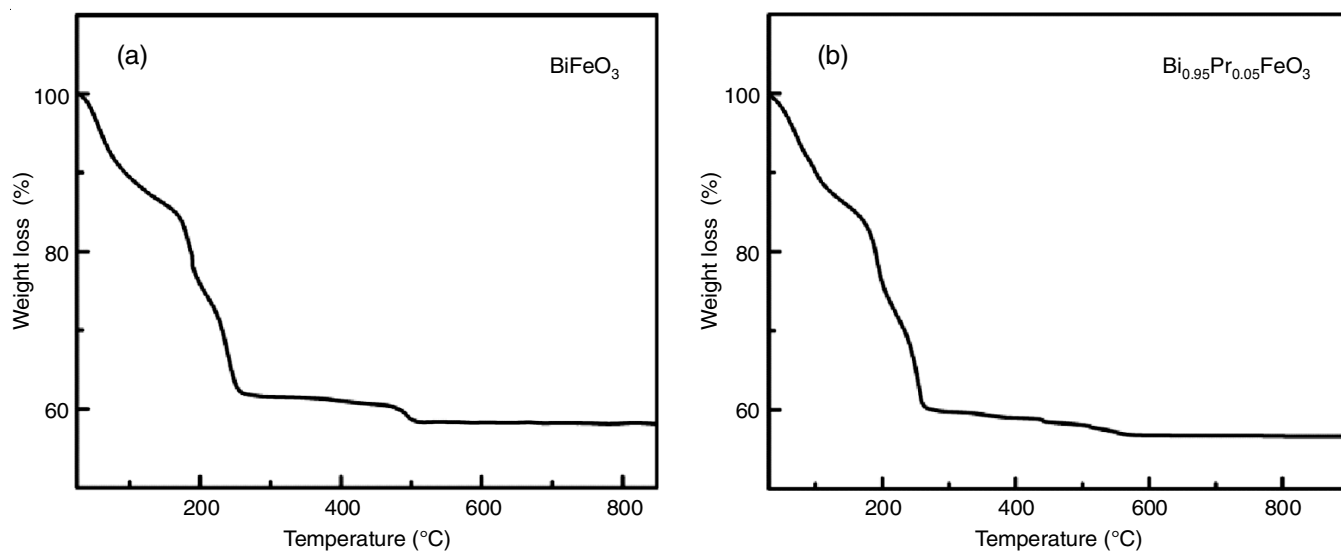


Fig. 1. (a) Thermograms of BiFeO_3 precursor powder (a) and $\text{Bi}_{0.90}\text{Pr}_{0.10}\text{FeO}_3$ precursor powder (b)

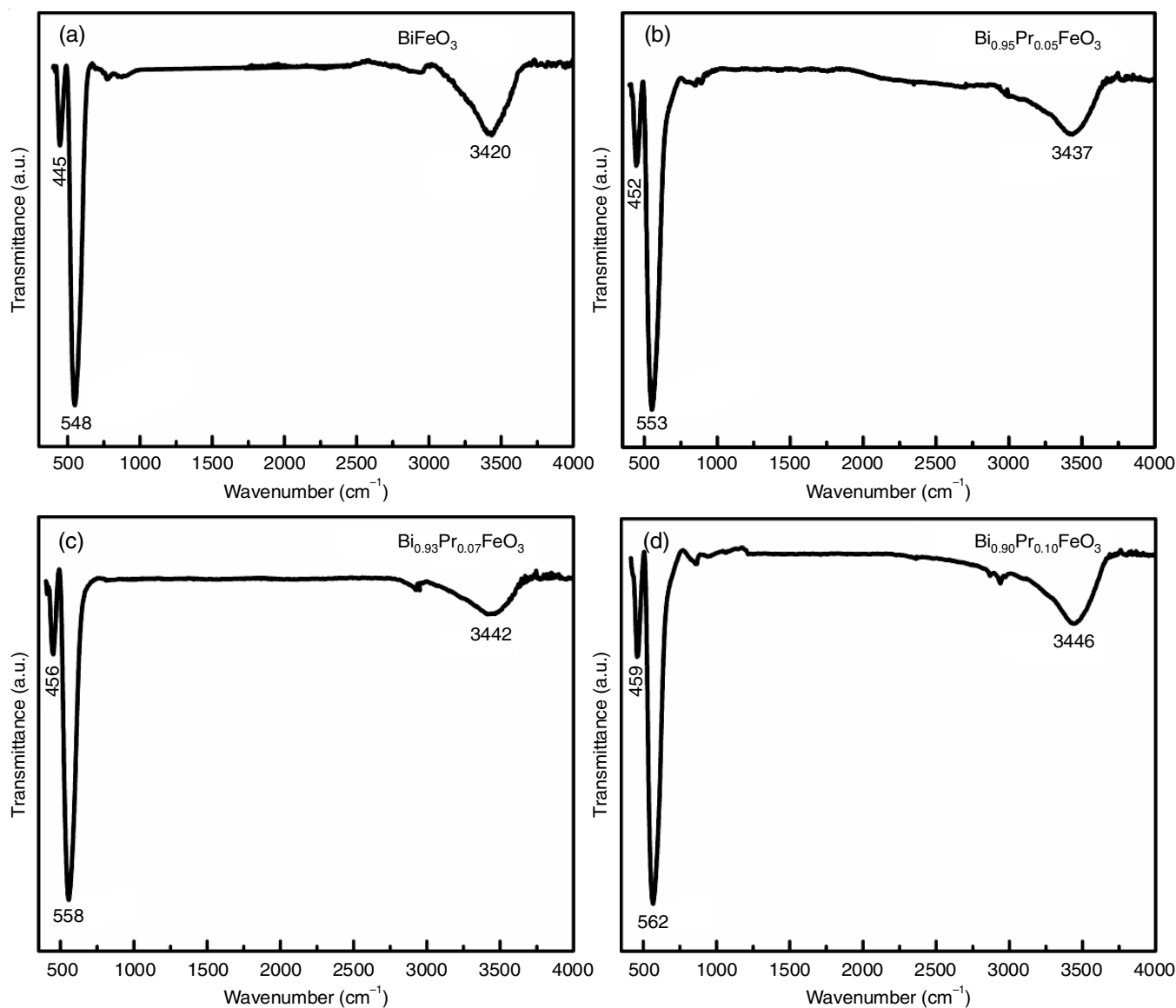


Fig. 2. FTIR spectra for (a) BiFeO_3 , (b) $\text{Bi}_{0.95}\text{Pr}_{0.05}\text{FeO}_3$, (c) $\text{Bi}_{0.93}\text{Pr}_{0.07}\text{FeO}_3$ and (d) $\text{Bi}_{0.90}\text{Pr}_{0.10}\text{FeO}_3$ nanoparticles calcined at 400 °C

δ distortional vibrations of O-Fe-O angles of the octahedral FeO₆ group in the perovskite compounds [25,26]. The IR frequencies of the bands 548 cm⁻¹ and 445 cm⁻¹ in BiFeO₃ shift to higher frequencies on increasing the Pr concentration (Fig. 2). The IR bands at 548 cm⁻¹ and 445 cm⁻¹ in BiFeO₃ shifts to 553 cm⁻¹ and 452 cm⁻¹ in Bi_{0.95}Pr_{0.05}FeO₃, 558 cm⁻¹ and 456 cm⁻¹ in Bi_{0.93}Pr_{0.07}FeO₃ and 562 cm⁻¹ and 459 cm⁻¹ in Bi_{0.90}Pr_{0.10}FeO₃, respectively. This behaviour is attributed to the change in the reduced mass of the Fe-O oscillator with increasing Pr-content.

TEM analysis: Fig. 3 shows a typical TEM image of pure and Pr-doped BiFeO₃ nanoparticles synthesized at 400 °C. It is evident that the size of synthesized pure and Pr-doped BiFeO₃ particles are in the range of 30 to 80 nm and roughly spherical in shape. This clearly confirms the nanocrystalline nature of all the synthesized samples and samples are polycrystalline in nature.

XRD analysis: Powdered X-ray diffraction (XRD) was employed to analyze the phase and the crystal structure of the

synthesized Bi_{1-x}Pr_xFeO₃ nanoparticles (where $x = 0.0, 0.05, 0.07, 0.10$). Fig. 4 shows the XRD patterns of pure and Pr-doped BiFeO₃ nanoparticles in the 2 θ range between 20° to 60° at room temperature. The XRD pattern of the synthesized BiFeO₃ nanoparticles closely matches the standard JCPDS card no. 86-1518, which corresponds to the rhombohedral crystal structure with $R3c$ space group of the BiFeO₃ phase. The characteristic peaks in the XRD pattern of BiFeO₃ appear at specific 2 θ values of 22.43°, 31.77°, 32.09°, 37.67°, 38.97°, 39.50°, 45.77°, 51.34°, 51.77°, 56.38° and 57.03°, corresponding to the (012), (104), (110), (113), (006), (202), (024), (116), (112), (018) and (214) planes, respectively. From Fig. 4b-d, it is clear that the XRD pattern of the 5%, 7% and 10% of Pr-substituted BiFeO₃ nanoparticles closely resemble with the XRD pattern of the pure phase of BiFeO₃ nanoparticles. There is no additional diffraction peak appeared in the Pr-doped samples, which indicates the absence of secondary impurities or other phases in the synthesized samples. This confirms the effective dispersion

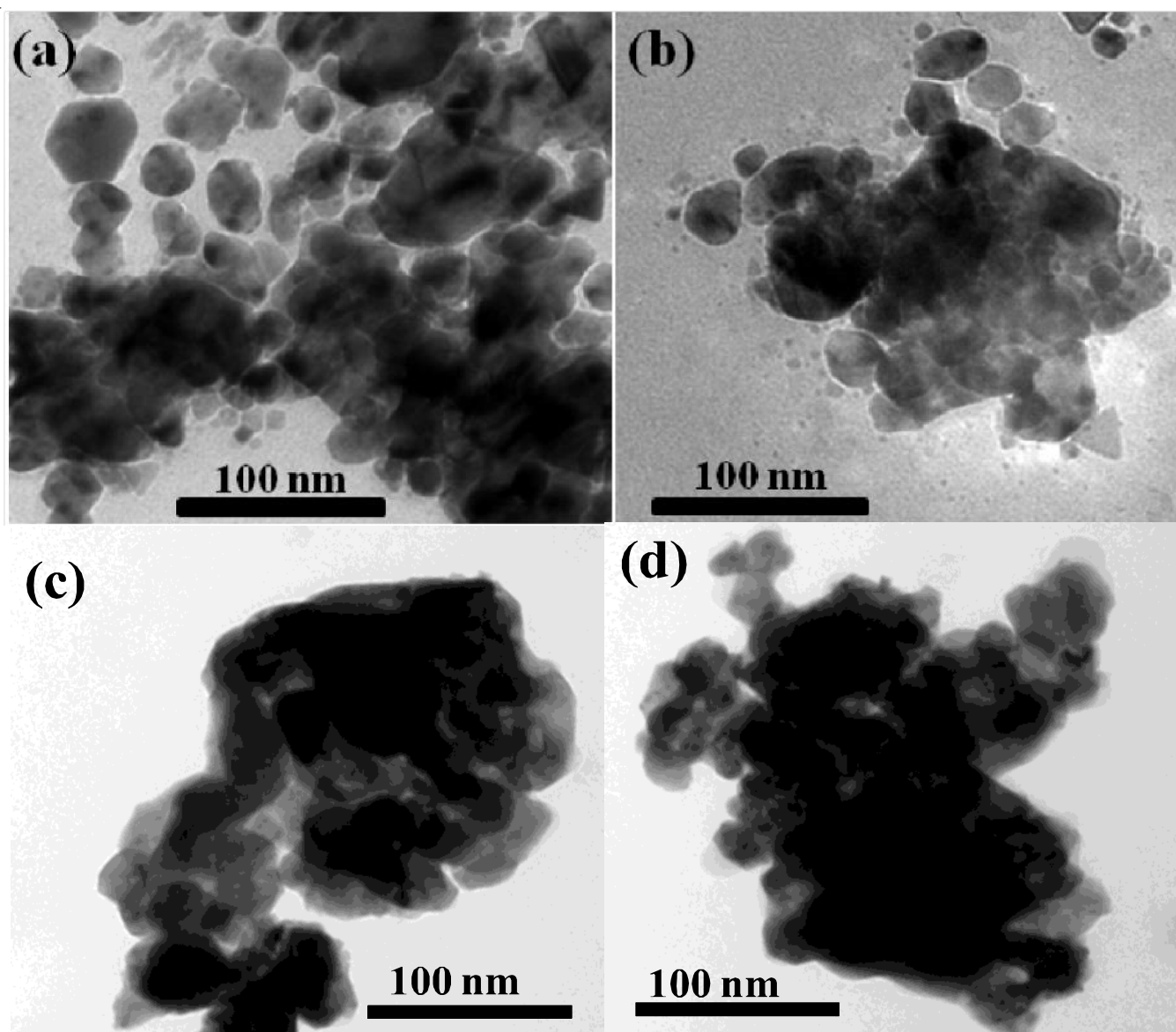


Fig. 3. TEM images of (a) BiFeO₃, (b) Bi_{0.95}Pr_{0.05}FeO₃, (c) Bi_{0.93}Pr_{0.07}FeO₃ and (d) Bi_{0.90}Pr_{0.10}FeO₃ nanoparticles calcined at 400 °C

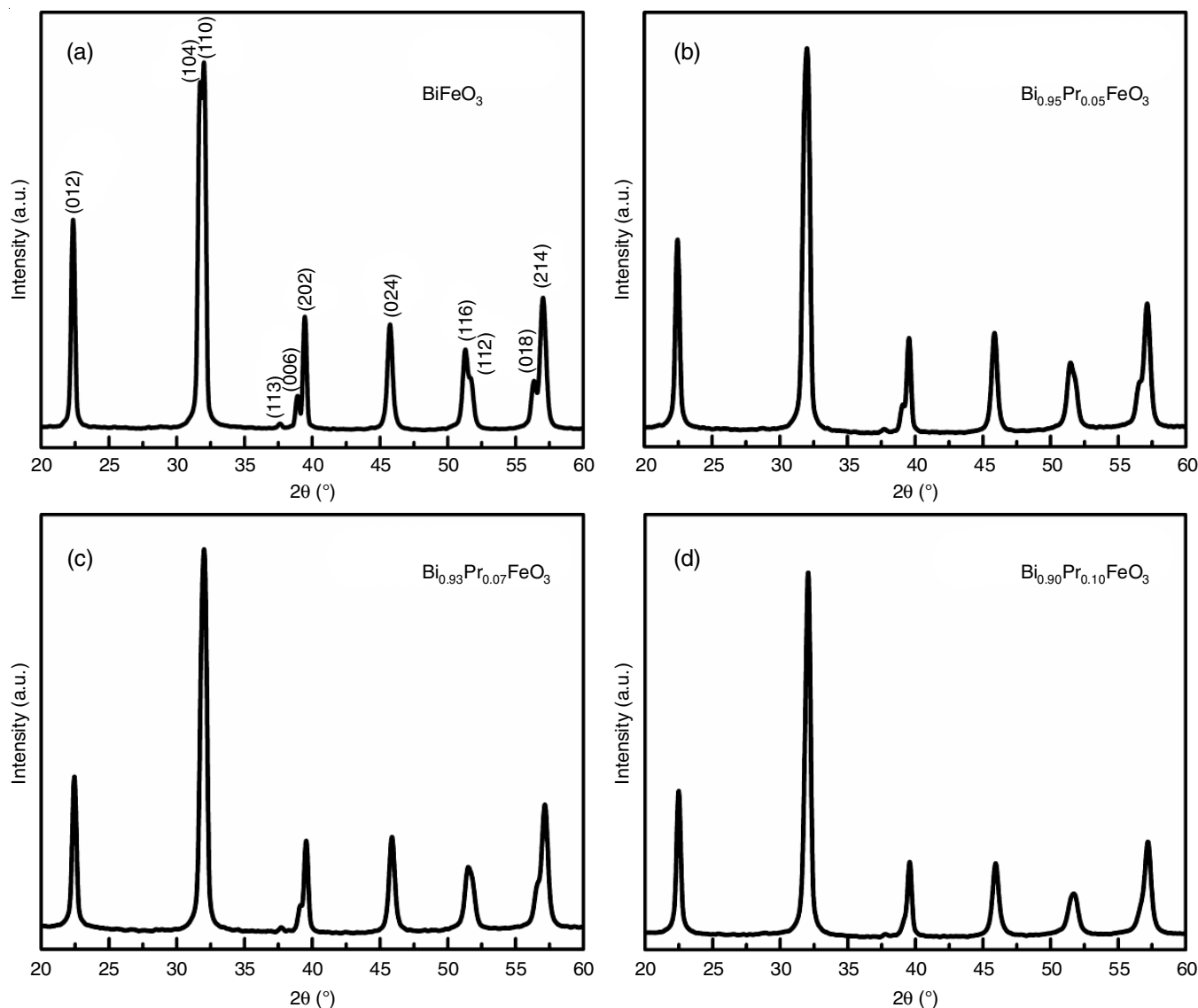


Fig. 4. XRD pattern of (a) BiFeO_3 , (b) $\text{Bi}_{0.95}\text{Pr}_{0.05}\text{FeO}_3$, (c) $\text{Bi}_{0.93}\text{Pr}_{0.07}\text{FeO}_3$ and (d) $\text{Bi}_{0.90}\text{Pr}_{0.10}\text{FeO}_3$ nanoparticles calcined at 400°C

of the Pr dopant within the BiFeO_3 host matrix and the successful formation of pure Pr-doped BiFeO_3 nanoparticles.

Further, there are two important effects of the Pr-doping in the BiFeO_3 matrix as observed in Fig. 4i. The diffraction peaks gradually shifted towards the higher 2θ and (ii) the splitted diffraction peaks in pure BiFeO_3 continuously merged in single peak on increasing Pr-concentration in BiFeO_3 matrix. To make these observations clearer, magnified XRD patterns in the vicinity of 2θ around 32° , 39° , 51° and 57° are shown in Fig. 5. It is confirmed that diffraction peaks corresponding to the hkl planes [(110) and (104)], [(006) and (202)], [(116) and (112)] and [(018) and (214)] of pure BiFeO_3 shifted gradually to higher 2θ values till 7% Pr-doping and merged in a single broad diffraction peak in 10% Pr-doped BiFeO_3 nanoparticles. This observed peak shifting and merging in the XRD pattern of $\text{Bi}_{1-x}\text{Pr}_x\text{FeO}_3$ nanoparticles with increasing Pr concentration suggests that there are partial structural changes occurs in the BiFeO_3 matrix. It reveals that Pr^{3+} ions occupy the Bi site in BiFeO_3 since the Shannon Prewitt ionic radius of Pr^{3+} (1.12 \AA ,

coordination no. 8) and for Bi^{3+} (1.17 \AA , coordination no. 8) are comparable within Goldschmidt tolerance limit [27]. This result suggests strain in lattice parameter and the rhombohedral structure is distorted by Pr-substitution. There exists a structural transformation and a gradual change in lattice constant from rhombohedral structure ($R3c$) to triclinic structure ($P1$), which is consistent with Sm-doped BiFeO_3 [28,29].

Further, a similar effect of doping of rare earth ions in BiFeO_3 has been reported by various researchers [16,30-35]. In addition, the crystalline sizes calculated from the XRD patterns using Scherrer's formula were found to be 32, 26, 24 and 21 nm for BiFeO_3 , $\text{Bi}_{0.95}\text{Pr}_{0.05}\text{FeO}_3$, $\text{Bi}_{0.93}\text{Pr}_{0.07}\text{FeO}_3$ and $\text{Bi}_{0.90}\text{Pr}_{0.10}\text{FeO}_3$, respectively. With increasing Pr-doping content, the crystalline size of Pr-doped BiFeO_3 gradually decreases, further indicating structural distortion in BiFeO_3 induced by Pr-doping.

Conclusion

In this work, $\text{Bi}_{1-x}\text{Pr}_x\text{FeO}_3$ ($x = 0, 0.05, 0.07$ and 0.10) nanoparticles were synthesized by facile sol-gel auto combustion

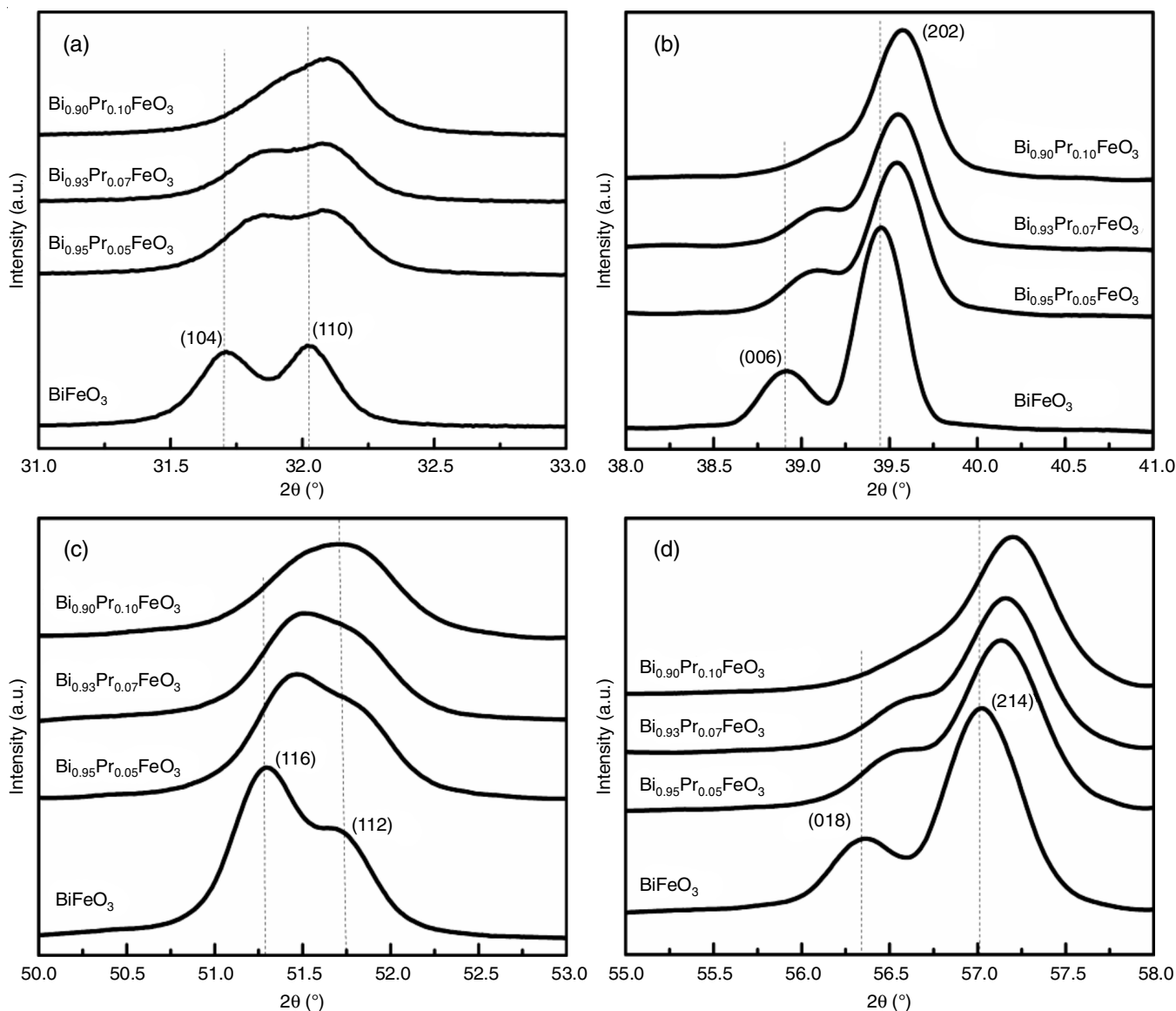


Fig. 5. The magnified XRD patterns in the vicinity of 2θ (a) 32° , (b) 39° , (c) 51° and (d) 57°

route using propylene glycol as a complexing agent after calcination at 400°C for 2 h. TGA results showed that the phase formation temperature for $\text{Bi}_{1-x}\text{Pr}_x\text{FeO}_3$ is 400°C . TEM results showed that prepared $\text{Bi}_{1-x}\text{Pr}_x\text{FeO}_3$ nanoparticles are nearly spherical in shape with their size ranges between 30–80 nm. The XRD analysis shows that pure perovskite rhombohedral BiFeO_3 phase with $R3c$ group and the structural phase transition exists on doping of Pr^{3+} in BiFeO_3 , as evident from the gradual shifting and merging of diffraction peaks. The average crystalline size was found to be 32 nm, 26 nm, 24 nm and 21 nm for BiFeO_3 , $\text{Bi}_{0.95}\text{Pr}_{0.05}\text{FeO}_3$, $\text{Bi}_{0.93}\text{Pr}_{0.07}\text{FeO}_3$ and $\text{Bi}_{0.90}\text{Pr}_{0.10}\text{FeO}_3$, respectively. The synthesized single phase $\text{Bi}_{1-x}\text{Pr}_x\text{FeO}_3$ nanoparticles can be used in various applications.

ACKNOWLEDGEMENTS

The authors gratefully acknowledge the University Department of Chemistry, Lalit Narayan Mithila University, Darbhanga for providing the research facilities. One of the authors, SKS,

acknowledges the University Grant Commission (UGC), New Delhi, India, for providing BSR start-up grants to carry out this research work.

CONFLICT OF INTEREST

The authors declare that there is no conflict of interests regarding the publication of this article.

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