

# Electronic Transitions, Inter- and Intra-Bond Interactions of an Azabicycle Single Crystal using DFT 

J. Dineshkumar ${ }^{1, \oplus}$, S. Subashchandrabose ${ }^{2, \oplus}$, S. Niaz ${ }^{3, ®}$ and P. Parthiban ${ }^{1, *, ©}$<br>${ }^{1}$ Department of Chemistry, Centre for R\&D, PRIST (Deemed University), Thanjavur-613403, India<br>${ }^{2}$ Department of Physics, Centre for R\&D, PRIST (Deemed University), Thanjavur-613403, India<br>${ }^{3}$ Department of Physics, University of Sargodha, Sub-campus Bhakkar, 30000, Pakistan<br>*Corresponding author: E-mail: parthisivam@yahoo.co.in

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#### Abstract

2,4-Diphenyl-3-azabicyclo[3.3.1]nonan-9-one O-benzyloxime (ABN-OBn) was synthesized by modified Mannich condensation, purified by recrystallization and single crystals were grown by slow evaporation from ethanol. The empirical formula of the molecule is $\mathrm{C}_{27} \mathrm{H}_{28} \mathrm{~N}_{2} \mathrm{O}$ as witnessed by HRMS, elemental analysis and the X-ray diffraction. The crystal belongs to triclinic system $(\alpha=73.640, \beta=78.505, \gamma=$ 87.078) with P-1 space group. The electronic excited states of ABN-OBn have been calculated using TD-DFT/B3LYP/6-31G(d,p) level of theory, in order to investigate the electronic transitions within the molecule. Frontier molecular orbitals (FMOs) of ABN-OBn have been studied to understand the electronic charge distributions and its band gap ( $5.0514 \mathrm{eV} / 245.45 \mathrm{~nm}$ ). Density of states (DOS), partial density of states (PDOS) and total density of states (TDOS) with respect to functional groups were computed to investigate the electron densities of functional groups in the molecule. Natural bond orbital (NBO) has been performed to explore the intramolecular $\pi$ - $\pi^{*}$ interaction of the compound.


Keywords: Azabicycle, Crystal structure, Hirshfeld surface analysis, Computational study, DFT.

## INTRODUCTION

Azabicyclononanes (ABNs) are present in the naturally occurring alkaloids, having a broad spectrum of medicinal activities such as antibacterial, antifungal, antituberculostic, analgesic, antioxidant, antitussive, anti-inflammatory, antipyretic, antiphologistic, sedatives, calcium antagonist, hypotensive, narcotic antagonism and local anesthetic, etc. [1-7].

By considering the importance, synthesis of ABNs is a parallel practice to the more complex isolation of ABN molecules in nature [8-11]. By optimized the modified Mannich reactions, we already reported a range of functionalized/highly functionalized ABNs [12-14]. In this article, we discussed the theoretical studies of the conveniently synthesized/biologically potent $\mathrm{ABN}-\mathrm{OBn}$ molecule (oxime ether derivative of ABN ); it contains functionalized ABN moiety and an active oxime ether pharmacophore of the Oxiconazole, an antifungal drug. It is a fact that the biological actions of any molecule mainly
depend on the stereochemistry of molecule and very significantly, the physico-chemical parameters are very vital in drug design, analysis and delivery [15-17].

Due to our interest in NMR spectral studies of oxime ethers of various nitrogen heterocycles [12-15,18-21], we synthesized and reported the complete ${ }^{1} \mathrm{H} \&{ }^{13} \mathrm{C}$ NMR spectral studies of a series of 2,6-diarylpiperidin-4-one O-benzyloximes, 2,4-diaryl-3-azabicyclo[3.3.1]nonan-9-one O-benzyloximes and 2,4,6,8-tetraaryl-3,7-diazabicyclo[3.3.1]nonan-9-one O-benzyloximes [12]. 2,4-Diphenyl-3-azabicyclo[3.3.1]nonan-9-one Obenzyl oxime ( $\mathrm{ABN}-\mathrm{OBn}$ ) is studied by computational analysis and compared with the crystallographic data. To our best, it is the first computational study for this class of bicyclic molecules of biological importance.

Further, we explored certain physico-chemical parameters (not only for the biological perspectives, even for material science applications) such as geometry of the molecule, structural property due to various functional groups, band gap, electronic excitations (in singlet and triplet) and their energy

[^0]transitions, non-linear optical activity using hyper-polar coefficient and electron density analysis.

## EXPERIMENTAL

Synthesis of 2,4-diphenyl-3-azabicyclo[3.3.1]nonan-9one (ABN): Mixture of cyclohexanone, benzaldehyde and ammonium acetate in 1:2:1.5 ratios in ethanol were gently warmed and stirred until the completion of the reaction. Thus, the formed crude product was filtered and washed with ethanol, ether (1:5) mixture [15]. The bicyclic ketone then recrystallized from ethanol to obtain pure compound.

Synthesis of 2,4-diphenyl-3-azabicyclo[3.3.1]nonan-9one O-benzyloxime (ABN-OBn): A mixture of 2,4-diphenyl-3-azabicyclo[3.3.1]nonan-9-one ( 5 mmol ), O-benzyl hydroxylamine hydrochloride ( 5 mmol ) and sodium acetate trihydrate ( 15 mmol ) in methanol was refluxed till completion of the reaction. After that water added to the reaction mixture and extracted with ether, dried with anhydrous sodium sulphate and evaporated. Thus, the obtained crude oxime ether ABNOBn was recrystallized from ethanol and slowly evaporated to obtain the diffraction quality crystals [15].

Computational details: The quantum chemical calculations of ABN-OBn were performed using the B3LYP level of theory supplemented with 6-31G(d,p) basis set, using Gaussian 03 program package invoking geometry optimization [22]. Initial geometry generated from geometrical parameters was minimized without any constraint in the potential energy surface at DFT level. Hirshfeld surface maps and fingerprint plots were generated from the crystallographic data using the Crystal Explorer 3.1 [23].

## RESULTS AND DISCUSSION

Molecular geometry: The ABN-OBn crystal structure belongs to a triclinic system $(\alpha=73.640, \beta=78.505, \gamma=87.078)$ with $\mathrm{P}-1$ space group. The lattice cell parameters are $\mathrm{a}=8.6884$ (7), $b=9.6961, c=14.1567(\AA)$ and the symmetry code of the molecule in the crystal unit is (i) $x-1 / 2,-y+1 / 2, z+3 / 2$; (ii) $x+1 / 2,-y+1 / 2, z-1 / 2$; (iii) $x+1, y, z-1$; (v) $x-1, y, z+1$. Crystallographic parameters are provided in Table-1. The conformation of piperidine and cyclohexane rings of the $\mathrm{ABN}-\mathrm{OBn}$ was analyzed with the puckering parameters (Table-2a), proposed by Cremer \& Pople [24]. Accordingly, conformation of the substituted piperidone ring (C1-C2-C3-C4-C5-N1) was found to be a chair with the total puckering amplitude $\mathrm{Q}_{\mathrm{T}}=$ $0.575(9) \AA$ and the phase angle $\theta=3.9(9)^{\circ}, \varphi=190^{\circ}(14)$; fairly deviated from the ideal chair of cyclohxane (for the ideal chair, $\mathrm{Q}_{\mathrm{T}}=0.630 \AA$ and $\theta=0^{\circ}$ or $180^{\circ}$ ) [24].

The conformation of cyclohexane (C2-C3-C4-C6-C7-C8) was also found to be a chair with the following puckering parameters, $\mathrm{Q}_{\mathrm{T}}=0.563(10) \AA, \theta=168.2^{\circ}(10), \varphi=240^{\circ}(5)$, which are significantly deviate from the ideal chair parameters than the piperidine ring. Hence, from the complete single crystal XRD analysis, it is confirmed that the molecule exists in a twin-chair conformation with equatorial disposition of both phenyl groups adjacent to the secondary amine group; the two benzene rings are inclined to each other at an angle of $115.86^{\circ}$ (calculated value is $115.8^{\circ}$ ). The bond parameters such

| TABLE-1 <br> CRYSTALLOGRAPHIC DATA AND STRUCTURE REFINEMENT PARAMETERS OF ABN-OBn |  |
| :---: | :---: |
| Identification code | ABN-OB |
| Chemical formula | $\mathrm{C}_{27} \mathrm{H}_{28} \mathrm{~N}_{2} \mathrm{O}$ |
| M | 396.51 |
| Crystal system | Tricilinic |
| Space group | P-1 |
| Temperature (K) | 273 (2) K |
| a, b, c ( $\AA$ ) | $\begin{aligned} & \mathrm{a}=8.6884(7) \AA, \mathrm{b}=9.6961(9) \AA, \\ & \mathrm{c}=14.1567(12) \AA \end{aligned}$ |
| $\alpha, \beta, \gamma\left({ }^{\circ}\right)$ | $\begin{aligned} & \alpha=73.640(5)^{\circ}, \beta=78.505(4)^{\circ}, \\ & \gamma=87.078(4)^{\circ} \end{aligned}$ |
| $\mathrm{V}\left(\AA^{3}\right)$ | 1121.35 (17) $\AA^{3}$ |
| Z, Calculated density | $2,1.174 \mathrm{Mg} / \mathrm{m}^{3}$ |
| Absorption coefficient | $0.071 \mathrm{~mm}^{-1}$ |
| F(000) | 424 |
| $\theta$ range for data collection | 1.53 to $28.31^{\circ}$ |
| Limiting indices | $\begin{aligned} & -11<=h<=11,-12<=k<=12, \\ & -18<=1<=18 \end{aligned}$ |
| Reflections collected/unique | 13758/4801 [R(int $)=0.0632]$ |
| Completeness to $\theta=25.00$ | 96.3 \% |
| Absorption correction | None |
| Refinement method | Full-matrix least-squares on $\mathrm{F}^{2}$ |
| Data/restraints/parameters | 4801/4/275 |
| Goodness-of-fit on $\mathrm{F}^{2}$ | 0.994 |
| Final R indices [ $\mathrm{I}>2 \sigma(\mathrm{I})$ ] | $\mathrm{R} 1=0.0758, \mathrm{wR} 2=0.1973$ |
| R indices (all data) | $\mathrm{R} 1=0.2555, \mathrm{wR} 2=0.2787$ |
| Largest diff. peak and hole | 0.273 and -0.197 e. $\mathrm{A}^{-3}$ |

TABLE-2a
PUCKERING PARAMETERS OF PIPERIDINE AND CYCLOHEXANE RINGS OF ABN-OBn CRYSTAL STRUCTURE

| Puckering parameters | $\mathrm{Q}_{\mathrm{T}}$ | $\theta$ | $\varphi$ |
| :--- | :---: | :---: | :---: |
| Piperidine ring | $0.575(9) \AA$ | $3.9^{\circ}(9)^{\circ}$ | $190^{\circ}$ |
| C1-C2-C3-C4-C5-N1) |  |  |  |
| Cyclohexane ring <br> $(\mathrm{C} 2-\mathrm{C} 3-\mathrm{C} 4-\mathrm{C} 6-\mathrm{C} 7-\mathrm{C} 8)$ | $0.563(10) \AA$ | $168.2^{\circ}(10)$ | $240^{\circ}(5)$ |

as bond length $(\AA)$, bond angle $\left({ }^{\circ}\right)$, dihedral angle $\left({ }^{\circ}\right)$ and hydrogen bonding interactions were measured. Bond parameters of ABN crystal structure were compared with computed values to understand the geometry of the molecule. The bond length of $\mathrm{C} s p^{2}-\mathrm{N} s p^{2}$ is reported [25] as $1.281 \AA$, for a general case. Accordingly, in this molecule, calculated and experimental value of C3-N29 (sp ${ }^{2}$ ) bond lengths are $1.280 \AA$ and $1.299 \AA$, respectively. The C-N $\left(s p^{3}\right)$ bond length is obtained as $1.468 \AA$ and $1.465 \AA$ from calculated and experimental methods [25]. Similarly, C-C $s p$ and $s p^{2}$ hybridized bonds are also lie in their characteristic bond length range. Due to the coincidence in geometrical parameters, molecular structure of single crystal and its optimized molecular structure are in good agreement with each other; molecular structures are shown in Fig. 1 (optimized) and Fig. 2 (XRD). The computed and experimental results are shown in Table-2b.

Molecular orbital theory: MO theory calculation was performed using the TD-DFT/B3LYP/6-31G(d,p) level of theory calculation, the results are presented in Table-3, in which the singlet excited states ( $n$ states $=6$ ) transitions were obtained (energy level diagrams of each transition are presented in Fig. 3a-f). The first excited state ( $\mathrm{ES}_{1}$ ) transition lies between HOMO


Fig. 1. Optimized molecular structure of $\mathrm{ABN}-\mathrm{OBn}$


Fig. 2. Crystal structure of ABN-OBn (CCDC No. 1861932)
$(\mathrm{H})$ and $\mathrm{LUMO}(\mathrm{L}), \mathrm{H} \rightarrow \mathrm{L}$, its excitation energy is $5.0514 \mathrm{eV} /$ 246 nm , in second excited state, there were six intermediate transitions occurred as shown in energy level diagram (Fig. 3a-f) its transition energy is calculated about $5.223 \mathrm{eV} / 237$ nm , whereas, the oscillator strength " f " of the transition is 0.0064. Of them, the intense transitions are $\mathrm{H} \rightarrow \mathrm{L}_{+2}$ and $\mathrm{H} \rightarrow \mathrm{L}_{+3}$ $(106 \rightarrow 109,106 \rightarrow 110)$, which is due to $2 p_{z}$ electron excitation in atoms 1-5, 15, 16 and 28-30 of the molecule. In $\mathrm{ES}_{3}$, there were seven combined electronic transitions as shown in Fig. 3c,

| TABLE-2bBOND PARAMETERS OF BOTH DFT (THEORETICAL)AND XRD (EXPERIMENTAL) STUDIES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Bond | Bond length ( $\AA$ ) |  | Bond | Angles ( ${ }^{\circ}$ ) |  |
|  | Theor. | Exp. |  | Theor. | Exp. |
| C1-C2 | 1.566 | 1.540 | C2-C1-C9 | 112.44 | 111.6 |
| C1-C9 | 1.520 | 1.520 | C2-C1-N28 | 110.27 | 110.1 |
| C1-N28 | 1.469 | 1.465 | C9-C1-N28 | 111.31 | 111.6 |
| C1-H32 | 1.107 | 0.980 | C1-C2-C3 | 106.30 | 107.4 |
| C2-C3 | 1.507 | 1.496 | C1-C2-C8 | 115.92 | 114.6 |
| C2-C8 | 1.550 | 1.543 | C3-C2-C8 | 108.16 | 108.5 |
| C3-C4 | 1.506 | 1.488 | C2-C3-C4 | 112.45 | 111.9 |
| C3-N29 | 1.280 | 1.299 | C2-C3-N29 | 128.84 | 129.0 |
| C4-C5 | 1.565 | 1.550 | C4-C3-N29 | 118.67 | 119.0 |
| C4-C6 | 1.549 | 1.507 | C3-C4-C5 | 106.56 | 107.2 |
| C5-C22 | 1.520 | 1.515 | C3-C4-C6 | 108.61 | 107.2 |
| C5-N28 | 1.468 | 1.465 | C5-C4-C6 | 115.86 | 115.8 |
| C6-C7 | 1.541 | 1.515 | C4-C5-C22 | 112.78 | 111.6 |
| C7-C8 | 1.541 | 1.518 | C4-C5-N28 | 110.01 | 109.2 |
| C15-C16 | 1.511 | 1.503 | C22-C5-N28 | 111.37 | 111.6 |
| C15-O30 | 1.436 | 1.454 | C4-C6-C7 | 113.95 | 114.9 |
| N29-O30 | 1.413 | 1.399 | C2-C8-C7 | 114.26 | 114.0 |
|  |  |  | C1-N28-C5 | 114.50 | 115.0 |
| TABLE-3 <br> SINGLET EXCITED ELECTRONIC TRANSITIONS OF ABN-OBn CRYSTAL |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Singlet excited electronic transitions |  |  | Band gap (eV/nm) | Oscillator strength |  |
| $\mathrm{H} \rightarrow \mathrm{L}$ |  |  | 5.0514/245.45 | 0.0747 |  |
| $\mathrm{H}_{-1} \rightarrow \mathrm{~L}$ |  |  | 5.2233/237.00 | 0.0064 |  |
|  |  |  | 5.2309/237.02 | 0.0016 |  |
| $\mathrm{H}_{2} \rightarrow \mathrm{~L}, \mathrm{H}_{-1}+\mathrm{L}$ |  |  | 5.2509/236.12 | 0.0211 |  |
| $\mathrm{H}_{-6} \rightarrow \mathrm{~L}, \mathrm{H}_{-2} \rightarrow \mathrm{~L}, \mathrm{H}_{-2} \rightarrow \mathrm{~L}_{+1}, \mathrm{H} \rightarrow \mathrm{L}_{+1}$ |  |  | 5.3017/233.86 | 0.0161 |  |
| $\mathrm{H}_{-9} \rightarrow \mathrm{~L}, \mathrm{H}_{-9} \rightarrow \mathrm{~L}_{+1}, \mathrm{H}_{-6} \rightarrow \mathrm{~L}, \mathrm{H}_{-4} \rightarrow \mathrm{~L}$ |  |  | 5.3846/230.26 | 0.0012 |  |

where the intense transition is $\mathrm{H}_{\rightarrow+3}(106 \rightarrow 110)$. Similarly in $\mathrm{ES}_{4}, \mathrm{ES}_{5}$ and $\mathrm{ES}_{6}$, the intense transition is due to atoms involved in HOMO (106) level and $\mathrm{L}_{+2}(109), \mathrm{L}_{+4}(111)$ and $\mathrm{L}_{+5}(112)$ levels, respectively. All the transition in $\mathrm{ES}_{3}, 2 \mathrm{p}_{z}, 3 \mathrm{~s}$ and $3 \mathrm{p}_{\mathrm{z}}$ electrons are majorly involved, especially the nitrogen $\left(\mathrm{N}_{29}\right)$ acquires more negative coefficient $\left(-0.1714-2 p_{z}\right.$, than the other atoms.

Frontier molecular orbital calculation was performed using B3LYP/6-31G(d,p) level of theory calculation. The HOMO mainly localizes on the azabicycle and LUMO locate on the phenyl rings. The band gap between HOMO and LUMO is -5.742 eV .

NBO analysis: The NBO analysis performed using B3LYP/ 6-31G(d,p) level of theory calculation. The natural atomic orbital (NAO) and natural bond orbital (NBO) analysis were performed using Gaussian NBO version 3.1. The obtained results are presented in Table-4. The core level atomic orbital population was calculated as 59.97 e and valence orbital population was calculated as 151.50 e , whereas, the total minimal basis is 211.47 e and Rydberg basis (Non-Lewis) was accounted as 0.523 e . The NBO analysis shows that the core electrons as 59.97e, valence Lewis electrons as 147.32e and total Lewis electrons as 207.30e.

Donor and acceptor bonds, electron densities and hyperconjugative ( $\mathrm{E}^{2}$ ) interaction energies are given in Table-4. In NBO investigation, we mainly concentrate on the $\pi-\pi^{*}$ inter-
(a) Excited state $(106 \rightarrow 107)$

(b) Excited state $2(106 \rightarrow 109,110)$


LUMO+2 (109)
(c) Excited state $3(106 \rightarrow 110)$


MO98
LUMO+3 (110)
(e) Excited state $5(106 \rightarrow 111)$


LUMO+3 (111)



LUMO+3 (110)
(d) Excited state $4(106 \rightarrow 109)$


MO98
LUMO+2 (109)
(f) Excited state $6(106 \rightarrow 112)$



LUMO+3 (112)

Fig. 3. Electronic transitions along with frontier molecular orbitals of ABN-OBn

| TABLE-4 <br> SECOND ORDER PERTURBATION THEORY ANALYSIS OF NBO BASIS FOR ABN-OBn |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bond type | Donor (i) | ED | Acceptor (j) | ED | ${ }^{\text {a }}$ E ${ }^{(2)} \mathrm{kJ} / \mathrm{mol}$ | ${ }^{\text {b }}$ E(j)-E(i) | ${ }^{\text {c }} \mathrm{F}(\mathrm{i}, \mathrm{j})$ |
| $\sigma-\sigma^{*}$ | C1-N28 | 1.98402 | C1-C9 | 0.02989 | 2.09 | 1.13 | 0.021 |
|  |  |  | C5-C22 | 0.02980 | 3.97 | 1.19 | 0.030 |
|  |  |  | C5-N28 | 0.02170 | 2.76 | 1.06 | 0.024 |
|  |  |  | C9-C14 | 0.02120 | 7.11 | 1.28 | 0.042 |
| $\sigma-\sigma^{*}$ | C3-N29 | 1.9889 | C2-C3 | 0.04434 | 9.58 | 1.33 | 0.050 |
|  |  |  | C3-C4 | 0.03027 | 6.99 | 1.33 | 0.042 |
|  |  |  | C15-O30 | 0.03057 | 7.66 | 1.20 | 0.042 |
| $\sigma$ - $\sigma^{*}$ | C3-N29 | 1.97213 | C1-C2 | 0.03879 | 7.82 | 0.67 | 0.032 |
|  |  |  | C2-C8 | 0.02293 | 7.70 | 0.70 | 0.032 |
|  |  |  | C4-C5 | 0.04039 | 9.46 | 0.67 | 0.035 |
|  |  |  | C4-C6 | 0.02449 | 9.62 | 0.70 | 0.036 |
| $\pi-\pi^{*}$ | C9-C10 | 1.65457 | C11-C12 | 0.33039 | 87.53 | 0.28 | 0.069 |
|  |  |  | C13-C14 | 0.32586 | 82.72 | 0.28 | 0.067 |
| $\pi-\pi^{*}$ | C11-C12 | 1.66720 | C9-C10 | 0.34427 | 82.51 | 0.28 | 0.067 |
|  |  |  | C13-C14 | 0.32586 | 85.98 | 0.28 | 0.068 |
| $\pi-\pi^{*}$ | C13-C14 | 1.67346 | C9-C10 | 0.34427 | 86.15 | 0.29 | 0.069 |
|  |  |  | C11-C12 | 0.33039 | 82.84 | 0.28 | 0.067 |
| $\pi-\pi^{*}$ | C16-C21 | 1.64483 | C17-C18 | 0.32681 | 86.86 | 0.28 | 0.068 |
|  |  |  | C19-C20 | 0.33368 | 86.27 | 0.28 | 0.068 |
| $\pi-\pi^{*}$ | C17-C18 | 1.66661 | C16-C21 | 0.34458 | 84.06 | 0.29 | 0.068 |
|  |  |  | C19-C20 | 0.33368 | 85.77 | 0.28 | 0.068 |
| $\pi-\pi^{*}$ | C19- C20 | 1.66261 | C16-C21 | 0.34458 | 84.73 | 0.29 | 0.068 |
|  |  |  | C17-C18 | 0.32681 | 83.93 | 0.28 | 0.067 |
| $\pi-\pi^{*}$ | C22-C27 | 1.65459 | C23-C24 | 0.32612 | 82.76 | 0.28 | 0.067 |
|  |  |  | C25-C26 | 0.33021 | 87.53 | 0.28 | 0.069 |
| $\pi-\pi^{*}$ | C23-C24 | 1.67384 | C22-C27 | 0.34400 | 86.11 | 0.29 | 0.069 |
|  |  |  | C25-C26 | 0.33021 | 82.72 | 0.28 | 0.067 |
| $\pi-\pi^{*}$ | C25-C26 | 1.66714 | C22-C27 | 0.34400 | 82.47 | 0.28 | 0.067 |
|  |  |  | C23-C24 | 0.32612 | 86.11 | 0.28 | 0.068 |
| $\sigma-\sigma^{*}$ | N29-O30 | 1.98186 | C3-C4 | 0.03027 | 21.58 | 1.19 | 0.070 |
| $\mathrm{n}-\sigma^{*}$ | nO30 | 1.88699 | C3-N29 | 0.13601 | 66.44 | 0.34 | 0.066 |

actions, where, $\pi$ is a donor and $\pi^{*}$ is an acceptor. This investigation indicates that the contribution of nitrogen atoms is less, especially, delocalization of energy during the interaction of nitrogen bonds ( $\sigma \mathrm{C} 1-\mathrm{N} 28, \sigma \mathrm{C} 3-\mathrm{N} 29$ and $\pi \mathrm{C} 3-\mathrm{N} 29$ ) is shown to be minimum in this molecule, whereas, carbon-carbon bond interactions obtained more $\mathrm{E}^{2}$ energy. For instance, charge delocalization between C9-C10 and C11-C12 has $87.53 \mathrm{~kJ} / \mathrm{mol}$ of energy. Similarly, the average energy of C-C interactions is $82 \mathrm{~kJ} / \mathrm{mol}$ for the whole molecule. On the other hand, oxygen atom has appreciable $\mathrm{E}^{2}$ energy during $\sigma \mathrm{N} 29-\mathrm{O} 30 \rightarrow \sigma^{*} \mathrm{C} 3-$ C 4 and $\mathrm{nO} 30{ }^{\prime} \rightarrow \pi^{*} \mathrm{C} 3-\mathrm{N} 29$ interactions and they are 21.58 and $66.44 \mathrm{~kJ} / \mathrm{mol}$, respectively.

Density of states (DOS): Using Multiwfn 3.4.1 version [26], density of states of ABN-OBn was studied. Density of states is an important concept of solid state physics, which represents the number of states in unit energy interval. In an isolated system, the energy levels are discrete, though the concept of DOS is insignificant in single isolated organic molecule, if the discrete energy levels are broadened to curve artificially, the DOS graph can be used as a valuable tool for analyzing the nature of electron density.

The original total density of states (TDOS) of isolated system can be written as:

$$
\begin{equation*}
\operatorname{TDOS}(\mathrm{E})=\sum_{\mathrm{i}} \delta\left(\mathrm{E}-\varepsilon_{\mathrm{i}}\right) \tag{1}
\end{equation*}
$$

where $\varepsilon$ is Eigen value set of single-particle Hamilton, $\delta$ is Dirac delta function. If $\delta$ is replaced by broadening function $\mathrm{F}(\mathrm{x})$, such as Gaussian, Lorentzian and pseudo-Voigt function, we get broadened TDOS [26].

In $\mathrm{ABN}-\mathrm{OBn}$, the molecular orbitals (MOs) are fragmented and plotted the electron density of each fragments as shown in Fig. 4. The vertical dashed line indicates Fermi energy level. The original DOS graph has discrete comb-like lines and in fact, it is difficult to distinguish the discrete lines. While broadening the discrete lines (the black curve is TDOS) it is convenient to realize the dense of energy levels distributed. Besides, the PDOS is separated as fragments f1-f4, the f1 (red curve) belongs to C1-C8 group, which has a considerable contribution in the HOMO level and the f2 (blue line) belongs to N28 and N29, shows a meager contribution, whereas, the f3 (pink line) with maximum contribution due to the presence of oxygen in the molecule. Similar to f1, the fragment f4 (C9C27/gray) also contributes a considerable electron density. In addition, the fragments f1 and f4 contribute to the unoccupied levels as well. On the whole, the OPDOS magnitude is much smaller than TDOS and PDOS.


Fig. 4. Density of states (DOS) with respect to functional groups in ABNOBn molecule

Non-linear property analysis: Theoretical investigation plays a substantial role in understanding the quantitative structure property relationship (QSPR), which is able to assist in designing novel NLO materials. A molecule to be NLO active, it is important to have high hyperpolarizability $\left(\beta_{0}\right)$ values. The calculated values of $\beta_{0}$ by finite field approach method are given in Table- 5 along with the corresponding components.

| TABLE-5HYPERPOLARIZABILITY $\left(\beta_{0}\right)$, POLARIZABILITY $(\alpha)$AND DIPOLE MOMENT $(\mu)$ OF ABN-OBn |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameters | Values | Parameters | Values |
| $\beta_{\mathrm{xxx}}$ | -129.87 | $\alpha_{x x}$ | 331.3206 |
| $\beta_{\text {xxy }}$ | -15.90 | $\alpha_{x y}$ | 14.1323 |
| $\beta_{\text {xy }}$ | 17.72 | $\alpha_{y y}$ | 322.4904 |
| $\beta_{\text {yyy }}$ | 19.29 | $\alpha_{x z}$ | 17.3651 |
| $\beta_{x x z}$ | -14.92 | $\alpha_{y z}$ | -10.7406 |
| $\beta_{\text {xyz }}$ | -51.82 | $\alpha_{z z}$ | 217.77 |
| $\beta_{y y z}$ | -24.03 | $\alpha$ | $0.726 \times 10^{-33}$ |
| $\beta_{\text {xzz }}$ | 56.04 | $\mu_{\text {x }}$ | $-0.205$ |
| $\beta_{y z z}$ | -50.31 | $\mu_{\mathrm{y}}$ | 0.189 |
| $\beta_{z z z}$ | 70.47 | $\mu_{z}$ | -0.139 |
| $\beta$ | $0.6881 \times 10^{-30} \mathrm{esu}$ | $\mu$ | 0.3113 Debye |
| *Urea (standard) $=0.3728 \times 10^{-30}$ esu |  |  |  |

For $\mathrm{ABN}-\mathrm{OBn}$, we have obtained high value of $\beta_{\mathrm{xxx}}, \beta_{\mathrm{xxy}}$ and $\beta_{\mathrm{xyy}}$ components (Table-5) thus indicating that there is a charge imbalance along the $y$-axis due to the high electronegative oxygen atom lying in the $\mathrm{X}-\mathrm{Y}$ plane. The $\beta_{0}$ value $\left(0.6881 \times 10^{-30} \mathrm{esu}\right)$ also indicates that the compound has very lower nonlinear optical property. This compound has lower $\beta_{0}$ coefficient but higher than that of urea. Urea is one of the prototype molecules used in the study of the NLO properties of molecular systems. Therefore, it is used frequently as a threshold value for comparative purposes [27].

Hirshfeld surface analysis: Hirshfeld surface (HSs) and 2D fingerprint plot as shown in Fig. 5a-j were generated using Crystal Explorer 3.1, based on the results of single crystal X-ray diffraction. The crystal packing builds through the N$\cdots \mathrm{H}-\mathrm{C}$ interactions, where the crystal units are in zigzag pattern by means of anti-parallel packing of molecules. The function of $d_{\text {norm }}$ is a ratio encompassing the distances of any surface point to the nearest interior $\left(d_{\mathrm{i}}\right)$ atom, exterior $\left(d_{\mathrm{e}}\right)$ atom and the van der Waals radii of the atoms [28]. The negative value of $d_{\text {norm }}$
indicates the sum of $d_{\mathrm{i}}$ and $d_{\mathrm{e}}$, which is shorter than the sum of the relevant van der Waals radii. It is considered to be in the closest contact and visualized as red in the Hirshfeld surface. The white colour denotes intermolecular distances closer to van der Waals contacts with $d_{\text {norm }}$ equal to zero, whereas contacts longer than the sum of van der Waals radii with positive $d_{\text {norm }}$ values are coloured as blue. A plot of $d_{\mathrm{i}}$ versus $d_{\mathrm{e}}$ is 2 D fingerprint plots that recognize the existence of different types of intermolecular interactions. In the shape index, the highlighted red and blue triangles shown by purple ellipse indicate that the $\pi \cdots \pi$ interactions identically present in the crystal structure and its 2D fingerprint shows the $72 \%$ contribution by $\mathrm{C} \cdots \mathrm{C}$ contact of the Hirshfeld surface. Red and blue triangles patterns show explicitly how the molecule overlaps and contact with one another. Red triangle represents the carbon atoms present in the benzene ring of molecule outside the surface, while blue represents the carbon atoms of benzene ring inside the molecule. The curvedness surface indicates the electron density surface curves around the molecular interactions [29]. Moreover, the flat green region separated by the blue edges in curvedness surface is another characteristic of $\pi \cdots \pi$ stacking. The deep red spots in the $d_{\mathrm{e}}$ surface are responsible for strong interactions of C-H (6.2\%), C-N (6.3\%) and C-O (3.8\%).

## Conclusion

The target ABN-OBn single crystal belongs to triclinic system with P-1 space group. From the XRD analysis, it is clear that the molecule exists in a twin-chair conformation with equatorial disposition of the substituents. The two benzene rings on both sides of the secondary amine group of the azabicycle are inclined to each other at an angle of $115.86^{\circ}$. From the puckering data $\left[\mathrm{Q}_{\mathrm{T}}=0.575(9) \AA\right.$ and $\left.\theta=3.9^{\circ}\right]$, it is concluded that the piperidone ring of the azabicycle is comparatively closer to the ideal chair conformation, whereas, the cyclohexane deviates significantly as witnessed by its $\mathrm{Q}_{\mathrm{T}}(0.563) \AA$ and $\theta$ $\left(168.2^{\circ}\right)$. According to computational data, among the electronic transitions $\mathrm{ES}_{1}$ to $\mathrm{ES}_{6}$ ( $\mathrm{n}=6$ states), $\mathrm{ES}_{3}$ transition plays a major role, where, the electron occupancies predominantly lie in $2 p_{z}, 3 s$ and $3 p_{z}$ orbitals owing to the presence of nitrogen $\left(\mathrm{N}_{29}\right)$, which has a higher negative coefficient ( -0.1714 e ) than the other atoms in the molecule. FMO analysis reveals that the highest occupied molecular orbital mainly localized on the azabicycle, whereas, the lowest unoccupied molecular orbital locates on the phenyl rings; the band gap was found to be -5.742 eV . NBO interaction shows that the $\mathrm{C}-\mathrm{C}$ bond obtained more $\mathrm{E}^{2}$ energy, whereas, the average energy of C-C inter-actions is $82 \mathrm{~kJ} / \mathrm{mol}$ for the whole molecule. In DOS analysis, fragment f1 (red curve) belongs to C1-C6 group has a consi-derable contribution in the HOMO level. This molecule has no significant $\beta_{0}$ value, which indicates that the compound has very lower optical behaviour. ABN-OBn crystal 2D fingerprint shows that the $\mathrm{C} \cdots \mathrm{C}$ contact contributes $72 \%$ Hirshfeld surface. On the whole, this molecule mainly driven by carboncarbon bonding and does not exhibit significant optical or electronic properties but the architecture of molecular structure is interesting with informative geometrical parameters.

Appendix A: Data collection [30-32]: APEX2 [30]; cell refinement: SAINT Bruker [30]; data reduction: SAINT Bruker


Fig. 5. Hirshfeld surface analysis of ABN-OBn
[30]; program(s) used to solve structure: SHELXS97 [31]; program(s) used to refine structure: SHELXL97 [31]; molecular graphics: ORTEP-3 [32]; software used to prepare material for publication: SHELXL97 [31].

## CONFLICT OF INTEREST

The authors declare that there is no conflict of interests regarding the publication of this article.

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