# Geometrical Optimization and Natural Bond Orbital Analysis of Relevant Structures in the Diastereoselective Cuprate Conjugate Addition Reaction of $\alpha, \beta$-Unsaturated Lactams using Density Functional Theory 

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#### Abstract

In this study, density functional theory calculations at the wB97XD/Def2TZVPP level were performed to analyze the mechanism underlying the cuprate conjugate addition reaction of $\alpha, \beta$-unsaturated lactams. The calculation results were well-aligned with those obtained experimentally-the keto-aminal and aldo-aminal, i.e. $\mathbf{2}$ and 1a, yield the syn- and anti-products, respectively. The diastereoselectivity reversal originates from the small differences in the structure of the reactants. The pyramidalization and C7N3C2 angle between the aminal carbon, nitrogen and carbonyl carbon are large in $\mathbf{2}$. The dihedral angle of the aminal oxygen, aminal carbon, nitrogen and carbonyl carbon, O8C7N3C2, is closer to $180^{\circ}$ in $\mathbf{2}$ than in $\mathbf{1 a}$. The NBO analysis revealed string interactions between the lone pair of N3 and carbonyl $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ bond. These results validate the assumption-the planarity around nitrogen in molecule $\mathbf{2}$ increases the nucleophilicity of the carbonyl oxygen, thereby driving the reaction between molecule 2 and trimethylsilyl chloride (TMSCl), which yields a siloxyiminium cation $\mathbf{5 b}$ and this $\mathbf{5 b}$ propels the syn addition of dimethylcuprate, leading to the formation of complex 7 . The $\pi(\mathrm{C} 5-\mathrm{C} 6)(\mathrm{HOMO})$ and $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)(\mathrm{LUMO})$ interactions in the siloxyiminium cation explain the increased $\mathrm{C} 5-\mathrm{C} 6$ double bond electrophilicity. The aldo-aminal 1a directly reacts with dimethylcuprate under steric control and yields the anti complex $\mathbf{6 a}$, whose $\pi$ character is stronger than that of the syn complex 7 and this weak $\pi$ characteristics of 7 increases its stability to compensate for the trimethylsilyl disturbance. The bicyclic $\alpha, \beta-$ unsaturated lactam 8 does not contain aminal oxygen and thus remains unreactive during the cuprate conjugate addition reaction. Moreover, its pyramidalization is higher than that of the keto-aminal 2 and its dihedral angle of C8C7N3C2 is closer to $180^{\circ}$. Finally, a thermodynamic anti product is obtained, which is more stable than the syn-product because of less torsional strain.


Keywords: Diastereoselectivity, Conjugate addition, $\alpha, \beta$-Unsaturated lactams, Density functional theory, Natural bond orbital.

## INTRODUCTION

Conjugate addition ( 1,4 -addition) to $\alpha, \beta$-unsaturated carbonyls, leading to the formation of $\mathrm{C}-\mathrm{C}$ bonds, is one of the most diverse reactions [1-6] and a crucial tool for organic synthesis. In addition, the Gilman reagent is one of the most outstanding reagent among its counterparts for this reaction. For example, lithium dimethylcopper $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CuLi}$ can be prepared by adding copper(I) iodide to methyllithium in tetrahydrofuran at $-78^{\circ} \mathrm{C}$ and this nucleophilic reagent reacts with electrophiles like $\alpha, \beta$-unsaturated carbonyl as illustrated in Scheme-I.

Wright et al. [7,8] investigated the stereochemical outcome of the conjugate addition of organocopper reagents to


Scheme-I: 1,4-Addition of $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CuLi}$ to cyclohex-2-enone
bicyclic $\alpha, \beta$-unsaturated lactams derived from pyroglutaminol in the presence of trimethylsilyl chloride ( TMSCl ). According to their foundations, the stereochemistry of the product depends on the structure of the reactants. If the reaction is triggered with the addition of the reactant aldo-aminal $\mathbf{1}$, then an anti product

[^0]is obtained, whereas keto-aminal 2 as a reactant yields a syn product as shown in Scheme-II.


Scheme-II: Conjugate addition of $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CuLi}$ to a,b-unsaturated bicyclic lactams 1 and 2

In a previous study, the syn-conjugate addition mechanism was adopted to synthesise inhibitors of interleukin-1 receptor associated kinase 4 (IRAK4) [9-11]. Wright et al. [7-9] suggested two different routes to elucidate the reversal of diastereo-selection. The syn-conjugate addition mechanism involves the formation of siloxyiminium ions followed by their comple-xation with copper depicted in Scheme-III. Since dimethyl-cuprate reacts with trimethylsilyl derivative, the TS$\mathbf{1}$ structure is preferentially produced, which can be attributed to stereo-chemistry and leads to the formation of a syn product.




Scheme-III: syn-Conjugate addition

By contrast, during the anti-conjugate addition, the formation of the cuprate complex precedes the TMSCl coordination step, which then yields a sterically preferential anti structured
product as illustrated in Scheme-IV. The observed differing diastereoselectivities can be attributed to the geometric structures of the reactants. X-ray-based analyses revealed that [7] the C7N3C2 angles in $\mathbf{1}$ and $\mathbf{2}$ are $122^{\circ}$ and $127.5^{\circ}$, respectively, Fig. 1, which implies that the structure of $\mathbf{2}$ is more planar around nitrogen than that of $\mathbf{1}$. Furthermore, because of the pyramidalization of the nitrogen atoms [12], the sums of the $\mathrm{C}-\mathrm{N}-\mathrm{C}$ bond angles are $343.4^{\circ}$ and $348.9^{\circ}$ in $\mathbf{1}$ and 2, respectively. Notably, as the angle value approaches $360^{\circ}$, the planarity of the structure increases. Finally, the dihedral angle formed by the 08 C 7 N 3 C 2 atoms in $\mathbf{2}\left(137.3^{\circ}\right)$ is larger than that in $\mathbf{1}$ (130.3 ${ }^{\circ}$ ) [13].


Fig. 1. Skeleton of $\alpha, \beta$-unsaturated bicyclic lactams

Although these geometrical differences are insignificant, the diastereoselectivity essentially changes, implying that the aldo-aminal, i.e. $\mathbf{1}$ yields an anti product, whereas the ketoaminal, i.e., $\mathbf{2}$, induces the formation of a syn product. Wright et al. [7] termed this phenomenon as "small change, big impact". The small planetary changes around the nitrogen atoms significantly affects the stereoselectivity. Because of the more planar structure of 2, structure $\mathbf{B}$ donates more to the resonance hybrid [14] as shown in Fig. 2. In addition, the oxygen atom becomes more nucleophilic and easily reacts with TMSCl to produce the siloxyiminium derivative and thus, the reaction progresses toward syn addition.


Fig. 2. Resonance structures of $\alpha, \beta$-unsaturated bicyclic lactams
Furthermore, the reduction potentials of $\alpha, \beta$-unsaturated carbonyl compounds play a crucial role in determine the reaction products. According to House et al. [15,16], 1,4-conjugate addition reaction of $\alpha, \beta$-unsaturated carbonyl compounds


Scheme-IV: anti-Conjugate addition
proceeds when the reduction potential is in the range from -1.2 to -2.4 V . When the reduction potential is higher (i.e. less negative) than -1.2 V , saturation of the $\alpha, \beta$-unsaturated carbonyl compound is observed, whereas no reaction with cuprate occurs when the reduction potential is lower (i.e., more negative) than -2.4 V.This study was focused on the geometrical optimization and natural bond orbital (NBO) analysis of selected structures involved in the diastereoselective cuprate conjugate addition reaction of $\alpha, \beta$-unsaturated lactams. Density functional theory (DFT) calculations were performed to gain insights into the diastereoselective mechanism that drives this addition reaction.

## COMPUTATIONAL METHODS

Density functional theory (DFT) calculations were performed using the Gaussian 16 software [17] and GaussView 6.0 interface [18]. All the geometric optimizations and frequency calculations were performed using the wB97XD-DFT method, which included empirical dispersion and long-range corrections. The valence and triple zeta Def2TZVPP was utilized as the basis set and all the stationary points were identified as minima (zero imaginary frequencies). The NBO calculations were performed at the same level of theory. The values of the total energy with thermal correction $(\Delta \mathrm{E})$, enthalpy $(\Delta \mathrm{H})$ and Gibbs energy $(\Delta \mathrm{G})$ were obtained under the standard conditions of 298.15 K and 1 atm in gas phase.

## RESULTS AND DISCUSSION

Diastereoselectivity strongly depends on the structure of the reactants and thus, the structures of $\mathbf{1 a}$ (aldo-aminal) and 2 (keto-aminal) were optimized and the resulting structures are shown in Fig. 3. Some of the associated geometric parameters are listed in Table-1. The N3-C2 length in $\mathbf{2}$ is slightly shorter than that in 1a, while that of $\mathrm{C} 2-\mathrm{O} 1$ in the former is slightly longer than that in the latter structure.

The C7N3C2 angle, pyramidalization and dihedral angle of O8C7N3C2 in 2 are consistent with those obtained via experiments [7] as well as higher than those in 1a, as evidenced

| TABLE-1 |  |  |
| :--- | :---: | :---: |
| SOME SELECTED GEOMETRIC PARAMETERS OF 1a AND 2 |  |  |
|  | Compound 1a | Compound 2 |
| Selected bond lengths ( $\AA$ ) |  |  |
| N3-C2 | 1.3838 | 1.3803 |
| C2-O1 | 1.2074 | 1.2089 |
| C7-N3 | 1.4608 | 1.4710 |
| O8-C7 | 1.4196 | 1.4322 |
| O8-C9 | 1.4116 | 1.4105 |
| C5-C6 | 1.3283 | 1.3277 |
| C6-C2 | 1.4898 | 1.4913 |
| Selected bond angles $\left(^{\circ}\right.$ ) |  |  |
| C7N3C2 | 121.8942 | 127.5005 |
| C7N3C4 | 110.0705 | 110.2210 |
| C4N3C2 | 110.7588 | 111.2607 |
| Sum of CNC angles | $342.7235^{\circ}$ | $348.9822^{\circ}$ |
| (pyramidalization) | $-131.1902^{\circ}$ | $-137.3001^{\circ}$ |
| Dihedral angle of O8C7N3C2 |  |  |

from Table-1. These calculated results indicate that the planarity around nitrogen is higher in $\mathbf{2}$ than in $\mathbf{1 a}$ and validate the assumption (reported in previous studies) that the diastereoselectivity conjugate addition of cuprate to $\alpha, \beta$-unsaturated lactams depends on the planarity of nitrogen. Although the difference in C7N3C2 is only $5.6063^{\circ}$ and that in the pyramidalization is $6.2587^{\circ}$, these small changes reverse the addition type from syn for 2 to anti for $\mathbf{1}$. Because of the high planarity around the nitrogen in 2 , the nitrogen lone pair (LP) of electrons is donated to the carbonyl bond and this phenomenon increases the contribution of structure $\mathbf{B}$ to the resonance hybrid as shown in Fig. 2.

To examine the validity of this assumption, NBO analysis was conducted in the present study. NBO analysis is a robust tool for evaluating the interactions between the donor and acceptor orbitals of a molecule and provides significant insights into such bonding interactions. The stabilization energy $\mathrm{E}(2)$ associated with the electron delocalization between Lewis (filled) and non-Lewis (unfilled) NBOs is estimated as:

$$
\mathrm{E}(2)=\Delta \mathrm{E}_{\mathrm{i}, \mathrm{j}}=-\mathrm{q}_{\mathrm{i}} \frac{\mathrm{~F}^{2}(\mathrm{i}, \mathrm{j})}{\varepsilon_{\mathrm{i}}-\varepsilon_{\mathrm{j}}}
$$



Fig. 3. Optimized structures of 1a and 2
where $\mathrm{q}_{\mathrm{i}}$ is the donor orbital occupancy, $\varepsilon_{\mathrm{i}}$ and $\varepsilon_{\mathrm{j}}$ are diagonal elements and $F(i, j)$ is the Fock matrix element. The strength of the interactions between electron donors and acceptors is proportional to the stabilization energy $\mathrm{E}(2)$. The relevant NBO analysis results of 1a and $\mathbf{2}$ are presented in Tables 2 and 3, respectively.

TABLE-2 ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 1a
USING SECOND-ORDER PERTURBATION THEORY

| Donor <br> NBO $(\mathrm{i})$ | Acceptor <br> NBO $(\mathrm{j})$ | $\mathrm{E}(2)$ <br> $(\mathrm{kcal} / \mathrm{mol})$ | $\mathrm{E}(\mathrm{i})-\mathrm{E}(\mathrm{i})$ <br> $($ a.u. $)$ | $\mathrm{F}(\mathrm{i}, \mathrm{i})$ <br> $(\mathrm{a} . \mathrm{u})$. |
| :---: | :---: | :---: | :---: | :---: |
| $\pi(\mathrm{C} 5-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 24.04 | 0.44 | 0.097 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 36.77 | 0.81 | 0.157 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{C} 6)$ | 28.96 | 0.78 | 0.137 |
| LP (N3) | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 64.74 | 0.43 | 0.150 |
| LP (O8) | $\sigma^{*}(\mathrm{~N} 3-\mathrm{C} 7)$ | 3.52 | 0.78 | 0.047 |
| $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 52.85 | 0.02 | 0.073 |

TABLE-3

| TABLE-3 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 2 |  |  |  |  |
| USING SECOND-ORDER PERTURBATION THEORY |  |  |  |  |
| Donor | Acceptor | E(2) | E(i)-E(i) | F(i,i) |
| NBO $(\mathrm{i})$ | NBO $(\mathrm{j})$ | $(\mathrm{kcal} / \mathrm{mol})$ | $($ a.u. $)$ | $(\mathrm{a} . \mathrm{u})$. |
| $\pi(\mathrm{C} 5-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 23.61 | 0.44 | 0.096 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 36.91 | 0.82 | 0.157 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{C} 6)$ | 28.53 | 0.78 | 0.136 |
| LP (N3) | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 73.51 | 0.41 | 0.156 |
| LP $(\mathrm{O} 8)$ | $\sigma^{*}(\mathrm{~N} 3-\mathrm{C} 7)$ | 4.28 | 1.06 | 0.060 |
| $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 51.84 | 0.02 | 0.073 |

Tables 2 and 3 indicate that the strength of the interaction between the LP of N3 and $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ is the highest and the corresponding $\mathrm{E}(2)$ is $73.51 \mathrm{kcal} / \mathrm{mol}$ for 2 and $64.74 \mathrm{kcal} / \mathrm{mol}$ for 1a. In both compounds 1a and 2, the donor orbital is HOMO- 1 concentrate on N 3 , while the acceptor orbital is the LUMO carbonyl anti-bonding $\pi$.

The corresponding orbitals of 1a are illustrated in Fig. 4 and the same pattern is observed in the case of $\mathbf{2}$. No significant interactions are detected between the N3 LP and $\sigma^{*}(\mathrm{O} 1-\mathrm{C} 2)$. Because of this interaction between the nitrogen LP and carbonyl group, the oxygen atom becomes sufficiently nucleophilic to react reversibly with TMSCl and yields the siloxyiminium ion.

Aldo-aminal 1a reacts only with active TMSBr or TMSI, although in the presence of TMSCl, it reacts first with the cuprate [7]. The optimized structures of the siloxyiminium cations 5a and 5b are depicted in Fig. 5 and Table-4 presents some of their selected geometric parameters.

| TABLE-4   <br> SOME SELECTED GEOMETRIC PARAMETERS OF 5a AND 5b   |  |  |
| :---: | :---: | :---: |
| $\mathbf{5 a}$ |  |  |
| Selected bond lengths ( $\AA$ ) | $\mathbf{5 b}$ |  |
| N3-C2 | 1.3180 | 1.3160 |
| C2-O1 | 1.2724 | 1.2741 |
| C7-N3 | 1.4812 | 1.4942 |
| O8-C7 | 1.4057 | 1.4190 |
| O8-C9 | 1.4137 | 1.4123 |
| C5-C6 | 1.3376 | 1.3369 |
| C6-C2 | 1.4607 | 1.4621 |
| O1-Si | 1.7612 | 1.7556 |
| Selected bond angles $\left({ }^{\circ}\right)$ |  |  |
| C7N3C2 | 128.8347 | 132.3148 |
| C7N3C4 | 110.7001 | 110.7270 |
| C4N3C2 | 110.7312 | 110.7199 |
| C2O1Si | 132.2487 | 132.5785 |
| Sum of CNC angles (pyramidalization) | $350.2660^{\circ}$ | $353.7617^{\circ}$ |
| Dihedral angle $\left({ }^{\circ}\right)$ |  |  |
| O8C7N3C2 | -140.2599 | -145.7773 |
| N3C2O1Si | 179.9614 | 176.0670 |

In both $\mathbf{5 a}$ and $\mathbf{5 b}$, the nitrogen and silicon atoms are anti planar and are thus more stable than the syn conformation, while trimethylsilyl is located far from C7. The C7N3C2 angle, pyramidalization and dihedral angle of O8C7N3C2 in $\mathbf{5 b}$ are


Fig. 4. HOMO-1 and LUMO of 1a


Fig. 5. Optimized structures of the siloxyiminium cations 5a, 5b
larger than those in 5a, suggesting that the planarity around nitrogen is retained in the siloxyiminium cations as well. Further, preferred formation of $\mathbf{5 a}$ can be partially ascribed to its $\mathrm{O} 1-\mathrm{Si}$ bond, which is slightly shorter than that in $\mathbf{5 a}$, as evidenced from Table-4. Therefore, a detailed NBO analysis was conducted to evaluate the orbital interactions in $\mathbf{5 a}$ and $\mathbf{5 b}$ and the corresponding results are shown in Tables 5 and 6.

TABLE-5
ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 5a USING SECOND-ORDER PERTURBATION THEORY

| Donor NBO <br> $(\mathrm{i})$ | Acceptor <br> $\mathrm{NBO}(\mathrm{j})$ | $\mathrm{E}(2)$ <br> $(\mathrm{kcal} / \mathrm{mol})$ | $\mathrm{E}(\mathrm{i})-\mathrm{E}(\mathrm{i})$ <br> $(\mathrm{a} . \mathrm{u})$. | $\mathrm{F}(\mathrm{i}, \mathrm{i})$ <br> $(\mathrm{a} . \mathrm{u})$. |
| :---: | :---: | :---: | :---: | :---: |
| $\pi(\mathrm{C} 5-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 38.25 | 0.36 | 0.112 |
| $\sigma(\mathrm{O} 1-\mathrm{Si} 20)$ | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 8.39 | 1.41 | 0.098 |
| $\mathrm{LP}(\mathrm{O} 1)$ | $\sigma^{*}(\mathrm{C} 2-\mathrm{C} 6)$ | 16.32 | 1.06 | 0.118 |
| $\mathrm{LP}(\mathrm{O} 1)$ | $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 99.23 | 0.40 | 0.185 |
| $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 15.84 | 0.09 | 0.070 |
| LP $(\mathrm{O} 8)$ | $\sigma^{*}(\mathrm{~N} 3-\mathrm{C} 7)$ | 3.29 | 1.02 | 0.052 |
| $\sigma(\mathrm{C} 2-\mathrm{N} 3)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{Si} 20)$ | 3.07 | 1.28 | 0.057 |
| $\sigma(\mathrm{C} 4-\mathrm{N} 3)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 7.28 | 1.36 | 0.089 |
| $\sigma(\mathrm{C} 5-\mathrm{C} 6)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 5.61 | 1.39 | 0.079 |

TABLE-6
ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 5b USING SECOND-ORDER PERTURBATION THEORY

| Donor NBO <br> $(\mathrm{i})$ | Acceptor <br> $\mathrm{NBO}(\mathrm{j})$ | $\mathrm{E}(2)$ <br> $(\mathrm{kcal} / \mathrm{mol})$ | $\mathrm{E}(\mathrm{i})-\mathrm{E}(\mathrm{i})$ <br> $($ a.u. $)$ | $\mathrm{F}(\mathrm{i}, \mathrm{i})$ <br> $(\mathrm{a} . \mathrm{u})$. |
| :---: | :---: | :---: | :---: | :---: |
| $\pi(\mathrm{C}-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 37.54 | 0.37 | 0.112 |
| $\sigma(\mathrm{O} 1-\mathrm{Si} 23)$ | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 8.67 | 1.42 | 0.100 |
| $\mathrm{LP}(\mathrm{O} 1)$ | $\sigma^{*}(\mathrm{C} 2-\mathrm{C} 6)$ | 15.97 | 1.06 | 0.117 |
| $\mathrm{LP}(\mathrm{O} 1)$ | $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 97.09 | 0.41 | 0.184 |
| $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 16.24 | 0.09 | 0.071 |
| $\mathrm{LP}(\mathrm{O} 8)$ | $\sigma^{*}(\mathrm{~N} 3-\mathrm{C} 7)$ | 4.37 | 1.00 | 0.060 |
| $\sigma(\mathrm{C} 2-\mathrm{N} 3)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{Si} 23)$ | 3.17 | 1.28 | 0.058 |
| $\sigma(\mathrm{C} 4-\mathrm{N} 3)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 7.57 | 1.36 | 0.091 |
| $\sigma(\mathrm{C} 5-\mathrm{C} 6)$ | $\sigma^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 5.49 | 1.39 | 0.078 |

Two essential donor-acceptor interactions are observed in the $\mathbf{5 a}$ and $\mathbf{5 b}$ structures. First, the interaction between the donor LP of O1 (HOMO-2) and LUMO acceptor $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ can be ascribed to the negative O1, which is bonded to electro positive Si . Second, the critical interaction between $\pi(\mathrm{C} 5-\mathrm{C} 6)$ (HOMO) and $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ LUMO (Tables 5 and 6) increases the $\pi(\mathrm{C} 5-\mathrm{C} 6)$ electrophilicity in the siloxyiminium cation during the cuprate addition. The HOMO and LUMO of 5b are shown in Fig. 6.

Another hypothesis [7] for the diastereoselective cuprate conjugate addition reaction is the development of a positive charge on O8, which may attract the nucleophilic cuprate reagent. The recalculated NBO charges of some atoms in 2, $\mathbf{5 b}, \mathbf{1 a}$ and 5a are shown in Table-7. As the reaction proceeds from bicyclic $\alpha, \beta$-unsaturated lactams to siloxyiminium cations, the charge changes only negligibly, indicating that the effect of the charge on O8 on the cuprate addition mechanism is insignificant.

Moreover, Tables 5 and 6, indicate that the donor LP O8 weakly interacts with the acceptor $\sigma^{*}(\mathrm{~N} 3-\mathrm{C} 7)$ and may introduce some positive charges on O 8 . The siloxyiminium cation $\mathbf{5 b}$ undergoes syn reaction with dimethylcuprate and yields complex 7, whose optimized structure and some selected geometric parameters are presented in Fig. 7 and Table-8, respectively. During the addition of nucleophilic dimethylcuprate to $\mathbf{5 b}$, the $\mathrm{C} 2-\mathrm{C} 6$ and $\mathrm{O} 1-\mathrm{Si} 23$ bonds shorten, whereas the length of the C2-O1 and C5-C6 bonds increase because the negative dimethylcuprate moves the electron toward carbonyl. Correspondingly, the trimethylsilyl group drifts away from the copper space and finally, the Cu36-C5 bond becomes shorter than the Cu36-C6 bond because of the lateral bonding between $\mathrm{C} 41, \mathrm{C} 5$. Evidently, when the two methyl groups on copper are replaced with tert-butyl, the copper complex collapses because of steric hindrance. The internal interactions in complex 7 were investigated via NBO analyses and the corresponding results are shown in Table-9.


Fig. 6. HOMO and LUMO for 5a

| TABLE-7 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NBO CHARGES OF SOME ATOMS IN 2, 5b, 1a AND 5a |  |  |  |  |  |  |
| Species | O8 | C7 | N3 | C2 | O1 | C6 | C5 |
| $\mathbf{2}$ | -0.506 | 0.421 | -0.437 | 0.632 | -0.590 | -0.277 | -0.144 |
| $\mathbf{5 b}$ | -0.481 | 0.427 | -0.334 | 0.669 | -0.716 | -0.306 | -0.062 |
| $\mathbf{1 a}$ | 0.025 | 0.006 | 0.103 | 0.037 | -0.126 | -0.029 | 0.082 |
| $\Delta$ (charge) charge( $\mathbf{5 b}$ )-charge( $\mathbf{2}$ ) | -0.493 | 0.248 | -0.428 | 0.630 | -0.582 | -0.281 | -0.141 |
| $\mathbf{5 a}$ | -0.464 | 0.254 | -0.326 | 0.669 | -0.713 | -0.308 | -0.057 |
| $\Delta$ (charge) charge(5a)-charge(1a) | 0.029 | 0.006 | 0.102 | 0.039 | -0.131 | -0.027 | 0.084 |



Fig. 7. Optimized structure of complex 7

| TABLE-8 <br> SOME SELECTED GEOMETRIC PARAMETERS FOR COMPLEX 7 |  |  |  |
| :---: | :---: | :---: | :---: |
| Selected bo | hs ( $\AA$ ) | Selected bo | angles ( ${ }^{\circ}$ ) |
| N3-C2 | 1.3415 | C7N3C2 | 128.8337 |
| C2-O1 | 1.3041 | C7N3C4 | 111.0543 |
| C7-N3 | 1.4784 | C4N3C2 | 110.2149 |
| O8-C7 | 1.4156 | C2O1Si23 | 133.3319 |
| O8-C9 | 1.4199 | C6Cu36C41 | 138.2537 |
| C5-C6 | 1.4520 | C6Cu36C37 | 119.7792 |
| C6-C2 | 1.4026 | C5Cu36C41 | 96.5145 |
| O1-Si23 | 1.7053 | C5Cu36C37 | 161.7063 |
| Cu36-C5 | 1.9422 | C37Cu36C41 | 101.6978 |
| Cu36-C6 | 2.0680 | Dihedral angle ( ${ }^{\circ}$ ) |  |
| Cu36-C41 | 1.9591 | O8C7N3C2 | -151.0450 |
| Cu36-C37 | 1.9750 | N3C2O1Si23 | 154.9919 |
| Sum of CNC angles (pyramidalization) |  |  | $350.1029^{\circ}$ |

The $\sigma(\mathrm{C} 5-\mathrm{Cu} 36)$ bond is distributed around the neighbouring bonds and C6 and consequently, C5 becomes highly electrophilic for the C41 nucleophilic attack at the syn-face. The negative charge is concentrated on C 6 and the $\sigma(\mathrm{C} 41-$ Cu36) bond, i.e. HOMO-7, donates electrons to the acceptor $\sigma^{*}(\mathrm{C} 5-\mathrm{Cu} 36)$, i.e. $\mathrm{LUMO}+1$, leading to the formation of the


Fig. 8. HOMO-7 and LUMO +1 of complex 7

| TABLE-9 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS |  |  |  |  |
| FOR 7 USING SECOND-ORDER PERTURBATION THEORY |  |  |  |  |

$\mathrm{LP}=$ Lone pair of electrons
syn product 4. The HOMO-7 and LUMO+1 of complex 7 are depicted in Fig. 8.

The aldo-aminal (1a) directly reacts with dimethylcuprate in the presence of TMSCl and yields the anti-structure anion complex $\mathbf{6 a}$, whose optimized geometry and some structural parameters are shown in Fig. 9 and Table-10, respectively. The C 9 and Cu 20 are anti, which contribute to the stability of the complex. The C5-C6 exhibits double-bond characteristics and the geometry around nitrogen is less planner than that in the syn complex 7. The two methyl groups around copper are far


Fig. 9. Optimized structure of the anion 6a

| TABLE-10 |  |  |  |
| :---: | :---: | :---: | :---: |
| SOME SELECTED GEOMETRIC |  |  |  |
| PARAMETERS OF THE ANION 6a (anion) |  |  |  |

in $\mathbf{6 a}$, because in the absence of trimethylsilyl group, the complex is less crowded and thus, the structure is more relaxed.

The $\pi$-complex pattern of $\mathbf{6 a}$ is revealed by the NBO analysis as shown in Table-11. Although electrons are transferred


Fig. 10. HOMO and LUMO of complex $\mathbf{6 a}$

| ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 6a USING SECOND-ORDER PERTURBATION THEORY |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| Donor NBO <br> (i) | Acceptor NBO <br> (j) | $\begin{gathered} \mathrm{E}(2) \\ (\mathrm{kcal} / \mathrm{mol}) \end{gathered}$ | $\begin{gathered} \hline \mathrm{E}(\mathrm{i})-\mathrm{E}(\mathrm{i}) \\ (\text { (a.u.) }) \end{gathered}$ | $\begin{aligned} & \hline \mathrm{F}(\mathrm{i}, \mathrm{i}) \\ & (\text { (a.u. }) \end{aligned}$ |
| $\pi(\mathrm{C} 5-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 25.78 | 0.46 | 0.099 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 37.48 | 0.78 | 0.155 |
| LP (O1) | $\sigma^{*}$ (C2-C6) | 24.20 | 0.82 | 0.128 |
| LP (N3) | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 51.38 | 0.44 | 0.137 |
| $\pi^{*}$ (C5-C6) | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 86.55 | 0.05 | 0.086 |
| $\sigma(\mathrm{C} 2-\mathrm{C} 6)$ | LP*(6) (Cu20) | 11.39 | 1.06 | 0.101 |
| $\sigma(\mathrm{C} 4-\mathrm{C} 5)$ | LP ${ }^{\text {(6) }}$ ( (Cu20) | 10.57 | 1.04 | 0.096 |
| $\sigma(\mathrm{C} 5-\mathrm{C} 6)$ | LP**(6) (Cu20) | 29.97 | 1.07 | 0.164 |
| $\pi$ (C5-C6) | LP** (6) (Cu20) | 62.75 | 0.71 | 0.192 |
| $\sigma(\mathrm{C} 21-\mathrm{Cu} 20)$ | $\pi^{*}$ (C5-C6) | 17.87 | 0.41 | 0.087 |
| LP (5) (Cu20) | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 113.38 | 0.27 | 0.165 |
| LP (5) (Cu20) | $\sigma^{*}(\mathrm{C} 21-\mathrm{Cu} 20)$ | 17.00 | 0.65 | 0.105 |
| LP (5) (Cu20) | $\sigma^{*}(\mathrm{C} 25-\mathrm{Cu} 20)$ | 10.67 | 0.62 | 0.081 |
| LP* (6) (Cu20) | $\sigma^{*}(\mathrm{C} 25-\mathrm{Cu} 20)$ | 11.70 | 0.05 | 0.071 |
| $\mathrm{LP}=$ Lone pair of electron |  |  |  |  |

(donated) from C5-C6 to copper, a strong back donation ability from Cu (HOMO) to the LUMO, $\pi^{*}$ (C5-C6), is observed; this interaction is represented in Fig. 10. The orientation of C21 is suitable for its reaction with C5 and an anti product is derived in this process.

The presence of O8 in the $\alpha, \beta$-unsaturated lactams is crucial for the conjugate addition reaction. In compound $\mathbf{8}, \mathrm{O} 8$ is
replaced by a methylene group as shown in Fig. 11. The geometric data and NBO analysis results of $\mathbf{8}$ are provided in Tables 12 and 13, respectively. Interestingly, the pyramidalization in $\mathbf{8}$ is higher than that in $\mathbf{2}$ and the dihedral angle of C8C7N3C2 is closer to $180^{\circ}$. These results demonstrate that $\mathbf{8}$ is more planar around nitrogen, leading to strong interactions the nitrogen LP and $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$, as shown in Table-13. Although these strong interactions drive the reaction with TMSCl, the C5-C6 double bond electrophilicity is not sufficient for the reaction with the dimethylcuprate reagent.


Fig. 11. Optimized structure of $\mathbf{8}$

| TABLE-12 |  |
| :--- | :---: |
| SOME SELECTED GEOMETRIC PARAMETERS OF $\mathbf{8}$ |  |
| Selected bond lengths ( $\AA$ ) |  |
| N3-C2 | 1.3727 |
| C2-O1 | 1.2121 |
| C7-N3 | 1.4750 |
| C8-C7 | 1.5491 |
| C8-C9 | 1.5310 |
| C5-C6 | 1.3282 |
| C6-C2 | 1.4924 |
| Selected bond angles $\left({ }^{\circ}\right)$ | 127.1186 |
| C7N3C2 | 113.0001 |
| C7N3C4 | 111.6191 |
| C4N3C2 | $351.7378^{\circ}$ |
| Sum of CNC angles (pyramidalization) | $-147.3013^{\circ}$ |
| Dihedral angle of C8C7N3C2 |  |

TABLE-13
ANALYSIS OF THE FOCK MATRIX IN THE NBO BASIS FOR 8 USING SECOND-ORDER PERTURBATION THEORY

| Donor <br> NBO $(\mathrm{i})$ | Acceptor <br> NBO $(\mathrm{j})$ | $\mathrm{E}(2)$ <br> $(\mathrm{kcal} / \mathrm{mol})$ | $\mathrm{E}(\mathrm{i})-\mathrm{E}(\mathrm{i})$ <br> $($ a.u. $)$ | $\mathrm{F}(\mathrm{i}, \mathrm{i})$ <br> $(\mathrm{a} . \mathrm{u})$. |
| :---: | :---: | :---: | :---: | :---: |
| $\pi(\mathrm{C} 5-\mathrm{C} 6)$ | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 23.18 | 0.44 | 0.096 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{N} 3)$ | 35.27 | 0.83 | 0.155 |
| LP (O1) | $\sigma^{*}(\mathrm{C} 2-\mathrm{C} 6)$ | 28.52 | 0.78 | 0.135 |
| LP (N3) | $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | 80.20 | 0.40 | 0.160 |
| $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ | $\pi^{*}(\mathrm{C} 5-\mathrm{C} 6)$ | 51.91 | 0.02 | 0.074 |

Finally, the thermodynamic effect is evaluated. The assumed structures of the syn- and anti-products, which may form during the reaction of $\mathbf{2}$ or $\mathbf{1 a}$ with dimethylcuprate, are optimized and their thermodynamic parameters are calculated (Table-14). The anti product is more stable because of less torsional strain with C9. anti 3a is more stable than anti 4a and therefore, in the aldo-animal (1a), the anti face leads to the formation of a thermodynamic product because of steric control. However, in 2, because of the formation of siloxyiminium cation, the syn face is preferred for the cuprate addition, although this reaction yields a less stable product, viz. syn 4 (Fig. 12). In the presence of TMSCl , the formation of a siloxyiminium cation is observed in $\mathbf{2}$ but not in 1a. Therefore, the
trimethylsilyl transfer ability of $\mathbf{5 a}$ is expected to be stronger than that of $\mathbf{5 b}$ as confirmed by the calculations (Table-14, eqn. 3).

| TABLE-14 |  |
| :---: | :---: |
| STANDARD GIBBS ENERGY CHANGE |  |
| FOR SOME SELECTED REACTIONS |  |
| Reaction | $\Delta \mathrm{G}^{\circ}(\mathrm{kcal} / \mathrm{mol})$ |
| $\mathbf{4}(\mathrm{syn}) \rightarrow \mathbf{4 a}$ (anti) | -1.29 |
| $\mathbf{3 b}(\mathrm{syn}) \rightarrow \mathbf{3 a}($ anti) | -1.95 |
| $\mathbf{5 a}+\mathbf{2} \rightarrow \mathbf{5 b}+\mathbf{1 a}$ | -2.16 |

## Conclusion

In this study, the cuprate conjugate addition reaction of $\alpha, \beta$-unsaturated lactams was analyzed by DFT calculations at the wB97XD/Def2TZVPP level. The calculation results are in good agreement with the previously reported experimental ones, which demonstrated the reversal of diastereoselection from anti to $s y n$ while the reaction proceeds from aldo-aminal 1a to keto-aminal 2. Compared to 1a, $\mathbf{2}$ exhibits large C7N3C2 angle and pyramidalization, in addition to a $\sim 180^{\circ}$ dihedral angle O8C7N3C2. The NBO analysis revealed strong interactions between the LP of N3 and $\pi^{*}(\mathrm{O} 1-\mathrm{C} 2)$ bond. These foundations reinforce the assumption that the high planarity around nitrogen in $\mathbf{2}$ increases the nucleophilicity of the carbonyl oxygen, enabling the reaction between 2 and TMSCl, which yields siloxyiminium cations. In siloxyiminium cation, the nitrogen and silicon atoms are anti planar and this structure drives dimethylcuprate to attack the syn-face. Further, the increased C5-C6 double bond electrophilicity can be attributed to the $\pi(\mathrm{C} 5-\mathrm{C} 6)(\mathrm{HOMO})$ and $\pi^{*}(\mathrm{C} 2-\mathrm{N} 3)$ LUMO interactions in the siloxyiminium cation. The increased positive charge on O8 in the siloxyiminium cation may be attract the nucleophilic cuprate reagent, but its effect is negligible. The aldo-aminal (1a) directly reacts with dimethylcuprate under steric control to yield the anti complex $\mathbf{6 a}$, which exhibits superior $\pi$ characteristics compared to the syn complex 7 complex. This phenomenon endows additional stability to 7 to compensate for the


4 (syn)


Fig. 12. Optimized structures of $\mathbf{4}$ and $\mathbf{4 a}$
trimethylsilyl disturbance. The bicyclic $\alpha, \beta$-unsaturated lactam (8), which lacks aminal oxygen, is unreactive in the cuprate conjugate addition reaction. Its pyramidalization is higher than that of the keto-aminal (2) and the dihedral angle of C8C7N3C2 is closer to 180 . Furthmore, $\mathbf{8}$ is more planar around nitrogen and activates the reaction with TMSCl; however, the C5-C6 double bond electrophilicity is not sufficient for the reaction with dimethylcuprate. Thus, a balance between the nucleophilicity of the carbonyl oxygen and electrophilicity of $\mathrm{C}=\mathrm{C}$ is essential. The final anti product exhibits thermodynamical characteristics and is more stable than the syn product because of less torsional strain. Finally, the trimethylsilyl transfer ability of $\mathbf{5 a}$ is stronger than that of $\mathbf{5 b}$. The findings of this study are anticipated to propel more such investigations on method to isolate crucial copper complexes and gain more insights in to underlying mechanism of this interesting reaction.

## CONFLICT OF INTEREST

The authors declare that there is no conflict of interests regarding the publication of this article.

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