

## Study of Some Organic Superconductors Using BCS-Theory

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Using the conventional phonon exchange mechanism of superconductivity, we have succeeded in reproducing the transition temperature  $T_c$  of some newly discovered organic superconductors by introducing certain modifications to the well known BCS-formulae for  $T_c$ . Taking the value of density of states at the Fermi surface,  $N(o)$ , calculated from d.c. paramagnetic measurement, the values of  $\Delta_0(o)$  and  $H_c(o)$  have been evaluated in the weak coupling limit.

### INTRODUCTION

A new class of materials<sup>1,2</sup> based on the sulphur containing organic donor bis-(ethylidene-2-thio)-tetra-thiofulvalence (BEDT-TTF) has yielded over ten organic superconductors with the critical temperature  $T_c < 8$  K. Sugano<sup>3</sup> has discovered a new ambient-pressure organic superconductor (BEDT-TTF)<sub>2</sub>[Cu(NCS)<sub>2</sub>] with  $T_c = 10.4 \pm 0.3$  K by means of dc magnetic susceptibility measurements<sup>4,5</sup> and confirmed by resistivity measurements<sup>6</sup>. This material consists of sheets of the BEDT-TTF molecules with a zigzag arrangement of molecular dimers in the crystallographic bc plane and the sheets are interleaved by sheets of the [Cu(NCS)<sub>2</sub>]<sup>-</sup> ions<sup>7</sup>. Thus (BEDT-TTF)<sub>2</sub>[Cu(NCS)<sub>2</sub>] has a unique structure that does not form face to face stacking columns as found commonly in conventional organic conductors. It forms a two-dimensional interaction network where one dimer is nearly perpendicular to the neighbouring dimer. Since there is an unpaired electron per dimer, the unit dimer in [BEDT-TTF]<sub>2</sub>[Cu(NCS)<sub>2</sub>] may be regarded as an atom having one valence electron like alkali metals. Therefore (BEDT-TTF)<sub>2</sub>[Cu(NCS)<sub>2</sub>] is of great interest in the sense that it is not only the organic superconductor with highest  $T_c$  at present, but also the organic conductor with unique structural feature. Graebnes *et al.*<sup>8</sup> has performed high resolution specific heat-measurements on a single crystal of K-(BEDT-TTF)<sub>2</sub>Cu(NCS)<sub>2</sub> in magnetic field up to ST reveal a jump SC at  $T_c$ . Comparison with  $\gamma = 34$  mJ/mol K<sup>2</sup> derived from Pauli paramagnetism yields  $\Delta_c/\gamma T_c = 1.50 \pm 0.15$  within experimental error of the BCS value of 1.43. However, the magnetic penetration depth by muon-spin relaxation measurements<sup>9</sup>, suggests the superconducting

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pairing with line nodes in the energy gap. It is a big question whether the mechanism of organic superconductor can be explained by the BCS<sup>10</sup> theory or not. If one sticks to the measurements of surface impedance by Klein *et al.*<sup>11</sup> and Harshman *et al.*<sup>12</sup>, then these measurements suggest the conventional wave pairing.

In this paper, using conventional phonon exchange mechanism of superconductivity, we have succeeded in reproducing the transition temperature  $T_c$  of a large number of newly discovered organic superconductors. We have introduced certain modifications to the well known BCS-formula for  $T_c$ .

### Derivation of the modified BCS Formula for $T_c$

We start with the two familiar equations one for the superconducting energy gap parameters  $\Delta_0(0)$  and the other for the transition temperature  $T_c$  of the BCS theory which are given as<sup>13</sup>

$$\Delta_0(0) = \hbar w_D / \sin \hbar \left[ \frac{1}{N(o)V} \right], \quad (1)$$

and

$$\left( \frac{1}{N(o)V} \right) = \int_0^{\hbar w_D} \frac{dx}{x} \tanh \left( \frac{x}{2K_\beta T_c} \right), \quad (2)$$

For simple materials like Al, Cd etc. the values of Debye frequency  $\hbar w_D$  and the energy gap parameter at zero temperature are known from phonon dispersion measurements and the tunnelling measurements. With the help of (1) the value of the strength parameter  $g = [N(o)V]$  is determined.  $N(o)$  is the density of states at Fermi surface and  $V$  is the electron-phonon interaction potential. If one evaluates the integral of (2) keeping both  $T_c$  and  $\hbar w_D$  constant then  $N(o)V$  can be reproduced. In the case of organic superconductors  $\hbar w_D$  is not known experimentally. We conjecture that for organic superconductor the value of Debye temperature  $\theta_D$  at  $T = T_c$  is different from the value at  $T = 0$  K. Such temperature variation of  $\theta_D$  has been known for metallic systems like Al and Mg<sup>14</sup>. In order to account for the temperature variation of  $\theta_D$ , we assume that

$$\theta_D^{(c)}(T) = \theta_D^{(o)} \left[ 1 - \gamma \frac{T}{\theta_D^{(o)}} \right] \text{ for } T < T_c, \quad (3)$$

where  $\gamma$  is an adjustable parameter,  $\theta_D^{(c)}$  and  $\theta_D^{(o)}$  are the value of Debye temperature at  $T = T_c$  and  $T = 0$  K. The BCS formula for  $T_c$  in the weak coupling limit is given by

$$T_c = 1.14 \theta_D \exp [-1/g], \quad (4)$$

with the help of (3), the BCS formula (4) may be modified as

$$T_c^{(MBCS)} = \frac{1.14 \theta_D^{(o)} \exp [-1/g]}{[1 + 1.14\gamma \exp [-1/g]]}, \quad (5)$$

Using eqn. (5) we have calculated the transition temperature of organic super-

conductor. This has been given in Table-1. Using the BCS weak coupling limit, we have also calculated  $\Delta_0$  and  $H_{c0}$  for these superconductors given in Table-2.

TABLE-1

Organic Superconductor	$T_c$ (Expt) (K)	$\theta_D^{(0)}$ (K)	$g = N(o)V$	$\theta_D^{(0)}$ (K)	$\gamma$	TC[MBCS] (K)
(BEDT-TTF) <sub>2</sub> Cu[NCS] <sub>2</sub>	10.4	154	0.40	112	4.0	10.48
(BEDT-TTF) <sub>2</sub> Cu[N(CN) <sub>2</sub> ]CN	10.7	157	0.40	114	4.0	10.69
(BEDT-TTF) <sub>2</sub> Cu[N(CN) <sub>2</sub> ]Br	11.6	171	0.40	124	4.0	11.64
(BEDT-TTF) <sub>2</sub> Cu[N(CN) <sub>2</sub> ]Cl	12.8	188	0.40	137	4.0	12.80

TABLE-2

DENSITY OF STATE  $N(o) = 5.8 \times 10^{33} \text{ exp}^{-1} \text{ cm}^{-3}$

Organic Superconductor	Year of discovery	Country	$\Delta_0(o) = 1.76K_{\beta}T_c$ (lrg)	$H_{c0}^2(o) = 4\pi\Delta_0^2(o)N(o)$ (gauss)	$T_c$ (K)
(BEDT-TTF) <sub>2</sub> Cu[NCS] <sub>2</sub>	1988	U.S.A.	$2.52 \times 10^{-15}$	680	10.4
(BEDT-TTF) <sub>2</sub> Cu[H(CN) <sub>2</sub> ]CN	1991	Japan	$2.60 \times 10^{-15}$	702	10.7
(BEDT-TTF) <sub>2</sub> Cu[N(CN) <sub>2</sub> ]Br	1990	U.S.A.	$2.80 \times 10^{-15}$	756	11.6
(BEDT-TTF) <sub>2</sub> Cu[N(CN) <sub>2</sub> ]Al	1990	U.S.A.	$3.10 \times 10^{-15}$	837	12.8

## RESULTS AND DISCUSSION

In the present calculation, we have been able to obtain the transition temperature of some of the organic super-conductors by suitably modifying the well known BCS formulae for  $T_c$ . Taking the value of density of states  $N(o)$  calculated from d.c. paramagnetic susceptibility measurement the value of energy gap parameter  $\Delta_0(o)$  and critical field  $H_{c0}$  are determined. The phonon exchange mechanism can however be checked by evaluating various normal state properties of organic superconductors.

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