Application of the *ab initio* **Theory and PCM–UAHF Model for Prediction of the pKa for Formic and Silanoic Acids Derivatives in Aqueous Solution**

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> *Ab initio* molecular orbital methods at the CBSEQ level of theory have been used to study the structure and acidity of formic and silanoic acids derivatives in aqueous solution. The calculations are performed at the SCF level with inclusion of SCF–level thermochemical corrections to yield free energies of dissociation, using the basis sets 6- 31G** and the recently parametrized continuum–solvation method PCM–UAHF for the solvation contribution. The model furnishes pK_a values in relatively good agreement with experimental data. Scaling different parts of solvation energies provides a significant improvement in results and signifies the importance of balance of individual contributions from electrostatic, cavity, dispersion and repulsion interactions. The result shows that the investigated acids are weak and for C-acids the acidity increases in the order: $CCl_3COOH > FCOOH > CHCl_2COOH$ $>$ CH₂ClCOOH $>$ HCOOH $>$ NO₂COOH $>$ CH₃COOH $>$ NH2COOH > BrCOOH > ClCOOH; their Si-acidity order is: $CCl_3SiOOH > CHCl_2SiOOH > FSiOOH > CISiOOH >$ $HSiOOH > BrSiOOH > CH₂CISiOOH > CH₃SiOOH >$ $NO₂SiOOH > NH₂SiOOH$.

> **Key Words: pKa, Acidity, Formic acids, Silanoic acid, Solvation energy, Polarized continuum model,** *Ab initio* **calculations.**

INTRODUCTION

Quantitative structure–property relationships are mathematical equations relating chemical, biological and technological properties. QSPR models, once established, can be used to predict properties of compounds as yet unmeasured or even unknown. Thus, QSPR approach saves resources and expedites the process of development of new molecules $1,2$. The acidbase properties of organic molecules affect their toxicity³, chromatographic retention behaviour⁴ and pharmaceutical properties⁵. In addition the acidity constants play a fundamental role in many analytical procedures such as acid base titration, solvent extraction, complex formation and ion transport. Therefore, having the knowledge about acid–base properties of

4854 Rezaei–Sameti *Asian J. Chem.*

chemical substances gives an idea about their toxicity, pharmaceutical activity and analytical roles. Much of the theoretical foundation of modern physical organic chemistry is based on the observation of the effects on acid-base equilibrium of changing molecular structure⁶. Proton transfer reactions constitute an important class of chemical reactions and have been studied extensively over a long period of time⁷. These studies in a gas phase and solution phase provides information on inherent substitute effects and solute–solvent interactions. The study of acidities in the gas phase allows assessment of effects in the absence of the perturbing influence of solvent or counter ions $8-10$. The acidity of compounds in solution phase is also of interest since many reactions occur practically and experimentally in solution phase. Many biological systems use proton–transfer reactions to perform communication between the extra cellular and intracellular media and the rate of these reactions depends on the degree of dissociation of the $species¹¹$.

 For much smaller and congeneric series of compounds, solution–phase pK_a has also been correlated with gas–phase quantum chemical parameters^{12,13} and for 135 organic oxy acids a method for predicting dissociation constants was developed on the basis of empirically calculated atomic charges¹⁴. Previous investigations of the more fundamental approach of applying quantum chemical continuum–solvation methods^{15.16} for predicting solution–phase pK_a cover both semi empirical¹⁷⁻¹⁹ and *ab initio* treatments^{20,21}. The latter, however, were used only for a few compounds of small molecular size. As an overall result, acceptable correlations with relative pK_a trends were found within congeneric series of compounds, although the computational level was not sufficient to predict absolute pK_a values. Despite the gas–phase acidities, the calculations of acidities in solution phase are still deficient. This deficiency is due to the lack of a complete and precise model of solvation. Even recent models of solvation such as polarizable continuum model $(PCM)^{22}$ ignore some parts of solute–solvent interactions²³.

EXPERIMENTAL

The dissociation of an acid AH in aqueous solution²⁴,

$$
AH_{aq} + H_2O_{aq} \quad \Longleftarrow \quad A_{aq}^- + H_3O_{aq}^+ \tag{1}
$$

is governed by the equilibrium constant K, which is related to the dissociation constant K_a according to

$$
K = \frac{[A_{aq}^{-}][H_3O^{+}]}{[AH_{aq}][H_2O_{aq}]} = \frac{K_a}{[H_2O_{aq}]}
$$
 (2)

(It is assumed that concentrations can be used instead of the activities).

The associated free energy change ∆G can be written for 1 M solutions at 298 K as

$$
\Delta G_{(kcal/mol)} = -2.3RT \log K = 1.39 pK_a + 2.36
$$
 (3)

and correspondingly, the solution-phase dissociation constant pK_a is given by

$$
pK_a = 0.735 \Delta G - 1.735 \tag{4}
$$

where ∆G is the standard change in the Gibbs free energy for the process in water at 298.15 K.

$$
\begin{aligned} &\text{HA}_{g}+\text{CH}_{3}\text{COO}_{g}^{-}\xrightarrow{\Delta G^{0}_{gas}}\text{A}_{g}^{-}+\text{CH}_{3}\text{COOH}_{g}\\ &\downarrow \Delta G^{0}_{HA,sol}\downarrow \Delta G^{0}_{CH_{3}\text{COO}^{-},sol}\downarrow \Delta G^{0}_{A^{-},sol}\downarrow \Delta G^{0}_{CH_{3}\text{COOH,sol}}\\ &\text{HA}_{aq}+\text{CH}_{3}\text{COO}_{aq}^{-}\xrightarrow{\Delta G^{0}_{2}}\text{A}_{aq}^{-}+\text{CH}_{3}\text{COOH}_{aq} \end{aligned}
$$

Scheme-I. The thermodynamic cycle proposed to convert ΔG_{gas}^0 to ΔG

In order to calculate ∆G, we have used the thermodynamic cycle proposed by Namazian *et al.*²⁵, an isodesmic reaction, reaction (5) and the dissociation of acetic acid reaction (6) as reference molecule.

$$
HA_{aq} + CH_3COO_{aq}^- \longrightarrow A_{aq}^- + CH_3COOH_{aq} \tag{5}
$$

$$
CH_3COOH_{aq} + H_2O_{aq} \longrightarrow CH_3COO_{aq}^- + H_3O_{aq}^+ \tag{6}
$$

The Gibbs energy of reaction (1), ∆G can be written as a sum of Gibbs energy of reaction (5), ΔG_1 and Gibbs energy of reaction (6), ΔG_2 .

$$
\Delta G = \Delta G_1 + \Delta G_2 \tag{7}
$$

Scheme-I shows a thermodynamic cycle proposed to calculate the ΔG₁. From this cycle, ΔG_1 is given by following expression

 $\Delta G_1 = \Delta G_{1,gas} + \Delta G_{1,sol}$ (8)

in which ΔG_1 , sol is defined as follow:

$$
\Delta G_{1,\text{sol}} = \Delta G_{A^{\text{-}},\text{sol}} + \Delta G_{\text{CH}_3\text{COOH},\text{sol}} - \Delta G_{\text{HA},\text{sol}} - \Delta G_{\text{CH}_3\text{COO}_{\text{sol}}^{\text{-}}} \tag{9}
$$

The fourth term on the right-hand side of eqn. 9 represent free energies of solvation and have been computed with the recently developed *ab initio* continuum.solvation model PCM.UAHF²⁶. For the free energy of proton transfer in the gas phase, ∆G, computational models with high accuracy like the G2 model^{27,28} and complete basis set $(CBS)^{29}$ approaches would be typical methods of choice. For practical reasons, however, the following simplified approach was selected. The *ab initio* calculations have been performed at the level of Hartree-Fock. The zero-point energies and thermal corrections together with entropies have been used to convert the internal energies to the Gibbs energies at 298.15 K. A medium-size basis set, 6-31(d,p), has been chosen by considering the size of studied molecules. Higher level of theory was not justified because of hardware limitations and the significant length of time of computations. GAUSSIAN 98³⁰ have been employed for all *ab initio* calculations.

RESULTS AND DISCUSSION

The aim of present work is to provide a consistent and reliable set of gas phase and solvation phase acidities for C– and Si– acids R–MOOH [M $= C$, Si, R = H, F, Cl, Br, CH₃, CH₂Cl, CHCl₂, CCl₃, NH₂, NO₂ using at the Hartree Fock level of theory and 6-31(d, p) basis set and solvation energies obtained by PCM model. The calculated gas-phase energy and solvation energy of each acid and its corresponding anion together with the change of total standard Gibbs energy of reaction $(HA \rightarrow A^{-} + H^{+})$ is shown in Table-1. The change of Gibbs energy of deprotonation might be of theoretical interest, but only the differences between the most stable species can have physical meaning and can be compared with experiments. The

TABLE-1

GIBBS FREE ENERGY OF EACH MOLECULE AND ITS ANION IN THE GAS AND AQUEOUS PHASE TOGETHER WITH CHANGE OF GIBBS ENERGY, $\Delta G_{\rm gas}, \Delta G_{\rm sol}$ IN THE GAS PHASE AND SOLVATION PHASE

Compdound	$\Delta G_{\rm gas}$ (a.u.)		$\Delta G_{\rm sol}$ (a.u.)		$\Delta G_{\rm gas}$	$\Delta G_{\rm sol}$
	Acid	Anion	Acid	Anion	kcal/mol	
HSiOOH	-439.84080	-439.28837	-440.14956	-439.67834 346.655 295.665		
FSiOOH	-538.77351	-538.23304	-538.81839	-538.34830 339.144 298.450		
CISiOOH	-898.80610	-898.27737	-898.36770	-898.36770 331.783 295.959		
BrSiOOH	-3009.22032	-3008.69082	-3008.77643	-3008.77643 332.266 295.933		
CH ₃ SiOOH	-478.86930	-478.31303	-478.93240	-478.45710 349.065 304.430		
CH ₂ ClSiOOH	-937.77260	-937.22801	-937.82705	-937.35281 341.735 301.230		
CHCl ₂ SiOOH	-1396.66901	-1396.13687	-1396.70038	-1396.23149 333.917 294.227		
CCl ₃ SiOOH	-1855.55301	-1855.03431	-1855.57710	-1855.11146 325.483 292.168		
NH ₂ SiOOH	-494.90810	-494.34850	-494.96745	-494.48551 351.154 304.875		
NO ₂ SiOOH	-643.37200	-642.81061	-643.40132	-642.92512 352.278 304.466		
HCOOH	-188.74838	-188.18564	-188.77463	-188.30557 353.125 294.340		
FCOOH	-287.63155	-287.09544	-287.65018	-287.19790 336.414 283.807		
CICOOH	-647.66465	-647.18621	-647.66515	-647.17069 300.226 310.275		
BrCOOH	-2758.07280	-2757.60010	-2758.06753	-2757.58340 296.624 303.796		
CH ₃ COOH	-227.76917	-227.20573	-227.82690	-227.35240 353.564 297.751		
CH ₂ CICOOH	-686.67704	-686.12970	-686.71842	-686.25583 343.461 290.282		
CHCl ₂ COOH	-1145.57300	-1145.04120	-1145.60109	-1145.14620 333.710 285.448		
CCl ₃ COOH	-1604.45960	-1603.94080		-1604.47321 -1604.02100 325.552 283.766		
NH ₂ COOH	-243.79162	-243.22739	-243.84899	-243.37217 354.060 299.210		
NO ₂ COOH	-392.21164	-391.72286	-392.26231	-391.79071 306.714 295.931		

result shows that the acidities of acids in solvation phase is stronger than gas-phase. For C-acids studied CCl3COOH and for Si-acids studied CCl₃SiOOH is strongest acid.

Using the total Gibbs free energies, the pK_a values have been calculated using eqn. 4 and the results are shown in Table-2, where they are compared with those obtained from the experimental values. Inspection of calculated pK_a reveals that in most cases the pK_a values are reasonably close to the experimental values. For example, the calculated pK_a are 3.75 and 4.73 for formic acid and acetic acid, respectively whereas the experimental pK_a is reported to be 3.75 and 4.76. The data distribution of calculated values *vs.* experimental data for pK_a is shown in Fig. 1. In the some cases, large deviations are observed. These deviations are mainly because of solvation energies and they are for polar substituent such as halogen groups. The pK_a values are in the range of 0.74 for CCl₃COOH to 6.06 for NH2SiOOH. The experimental acidities of silanoic acid and its derivatives are not known. Therefore, it is not possible to compare the present theoretical results directly with experiments.

Compound	$\Delta G_{\rm 1gas}$ (kcal/mol)	$\Delta G_{\rm 1sol}$ (kcal/mol)	pK_{acal}	$pK_{\rm a,exp}$
HCOOH	-0.001	-0.005	3.75	3.75
FCOOH	-0.027	0.005	0.75	
CICOOH	-0.085	0.105	8.30	
BrCOOH	-0.091	0.100	6.45	
CH ₃ COOH	0.000	0.000	4.73	4.76
CH ₂ CICOOH	-0.016	0.004	2.59	2.86
CHCl ₂ COOH	-0.032	0.012	1.22	1.30
CCl ₃ COOH	-0.045	0.022	0.74	
NH ₂ COOH	0.001	0.002	5.14	
NO ₂ COOH	-0.075	0.072	4.20	
HSiOOH	-0.011	0.008	4.14	
FSiOOH	-0.023	0.019	3.94	
CISiOOH	-0.035	0.031	4.04	
BrSiOOH	-0.034	0.031	4.23	
CH ₃ SiOOH	-0.007	0.008	4.87	
CH ₂ ClSiOOH	-0.019	0.019	4.68	
CHCl ₂ SiOOH	-0.031	0.026	3.73	
CCl ₃ SiOOH	-0.044	0.036	3.14	
NH ₂ SiOOH	-0.004	0.011	6.06	
NO ₂ SiOOH	-0.002	0.004	5.04	

TABLE-2 GAS-PHASE AND SOLVATION ENERGIES AND pK, VALUES CALCULATED IN THIS WORK USING PCM MODEL

^aThe experimental values are taken from Ref. 24.

4858 Rezaei–Sameti *Asian J. Chem.*

Different solvation algorithms have been employed in order to calculate solvation energies. These models have been Dielectric-CPCM $(DPCM)^{31}$, Conductor-CPCM $(CPCM)^{32}$ and Integral equation Formalism-

 $CPCM$ (IEFPCM) 33 . These methods are different in their modeling of the cavity created in solvent in order to place the solute molecules. The isodensity surface, which is employed in the recent version of PCM methods, is a natural shape for the cavity and it corresponds to the reactive shape of molecules. The solvation energy of each molecule and its anion calculated using DPCM, CPCM and IEFPCM models are shown in Tables 3-5 as well as four components of solvation energies from the electrostatic interaction, cavity term, dispersion and repulsion energies. Examination of the calculated values shows that electrostatic interactions between anions and solvent are much greater than interaction of neutral molecules and solvent (seven to ten times for formic acid derivatives and two to three times for silanoic acids derivatives). Dispersion and repulsion energies of anions are also greater than acids because of the extra net charge on anions. Cavity energies of acids are slightly greater than anions because of the extra hydrogen atom. The overall calculated solvation energies of anions are of significant and play an important role in total solvation energy of reaction (5).

TABLE-4

4860 Rezaei–Sameti *Asian J. Chem.*

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