



## NOTE

### Simulation Studies on H<sub>2</sub>S Absorption in Potassium Carbonate Aqueous Solution Using a Membrane Module†

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Removal of H<sub>2</sub>S from H<sub>2</sub>S/N<sub>2</sub> gas mixture using a hollow-fiber membrane module is studied theoretically in this work. The absorption medium is aqueous solution of potassium carbonate. A mathematical model was developed to describe absorption of H<sub>2</sub>S in the module. Laminar parabolic velocity profile was used for the gas flow in the tube side; whereas, the liquid flow in the shell side was characterized by Happel's free surface model. The effect of various operating conditions on H<sub>2</sub>S removal is examined. The operating conditions examined included the gas flow rate, the liquid flow rate and the liquid concentration. The model was found to be efficient in prediction of membrane performance in gas absorption.

**Key Words:** Gas absorption, H<sub>2</sub>S, Hollow fiber, Mathematical model, Simulation.

Hydrogen sulfide (H<sub>2</sub>S) is a toxic gas and is also one of the major causes for environmental problems in chemical or petrochemical industries. It also has serious health effects associated with exposure of H<sub>2</sub>S<sup>1</sup>. The current H<sub>2</sub>S separation processes are based on physical and chemical processes including absorption, adsorption, cryogenic and membrane processes<sup>2</sup>. The separation of H<sub>2</sub>S through ordinary processes experiences a number of shortcomings such as channeling, flooding, entraining, foaming and also high capital and operating costs<sup>3,4</sup>. Recently, the gas-liquid hollow-fiber membrane contactors as gas absorption devices have become a subject of great interest<sup>4-8</sup>.

The main purpose of this study is to simulate H<sub>2</sub>S absorption through a hollow-fiber membrane contactor. The simulations are based on computational fluid dynamics of mass and momentum transfer in the liquid and gas phases.

#### Simulation of H<sub>2</sub>S absorption

**Formulation of mass transfer and absorption:** The model is developed for a segment of a hollow fiber, as shown in Fig. 1, through which the gas mixture flows with a fully developed laminar parabolic velocity profile. The fiber is surrounded by a laminar liquid flow in an opposite direction. Hydrogen sulfide gas is removed from the gas mixture by

diffusing through the membrane and then absorption and reaction with the solvent.

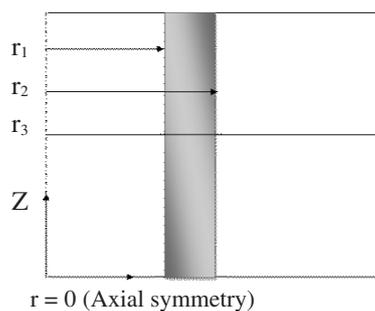


Fig. 1. Model domain

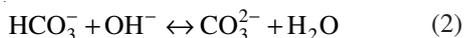
The continuity equation for each species in a reactive absorption system can be expressed as<sup>9</sup>:

$$\frac{\partial C_i}{\partial t} = -(\nabla \cdot C_i V) - (\nabla \cdot J_i) + R_i \quad (1)$$

where  $C_i$ ,  $J_i$ ,  $R_i$ ,  $V$  and  $t$  are the concentration, diffusive flux, reaction rate of species  $i$ , velocity and time, respectively. Either Fick's law of diffusion or Maxwell-Stefan theory can be used for the determination of diffusive fluxes of species  $i$ .

†This work is results of Azam Marjani's Ph.D. Thesis in Islamic Azad University, Tehran North Branch.

**Reaction rate for H<sub>2</sub>S absorption into K<sub>2</sub>CO<sub>3</sub> aqueous solution:** When the potassium carbonate is dissolved in water it is ionized into the potassium ion and carbonate ion. The bicarbonate ion and hydroxyl ion are then generated by the reactions in following reaction scheme.



The COMSOL multiphysics software is used to solve the differential equations set, by the finite element method and the direct linear system solver UMFPAK.

**Effect of gas and liquid flow rates on the removal of H<sub>2</sub>S:** The per cent H<sub>2</sub>S removal for different values of gas flow rates (the effect of convection term) is presented in Fig. 2. The increase in the gas flow rate reduces the residence time in the module, which in turn reduces the removal rate.

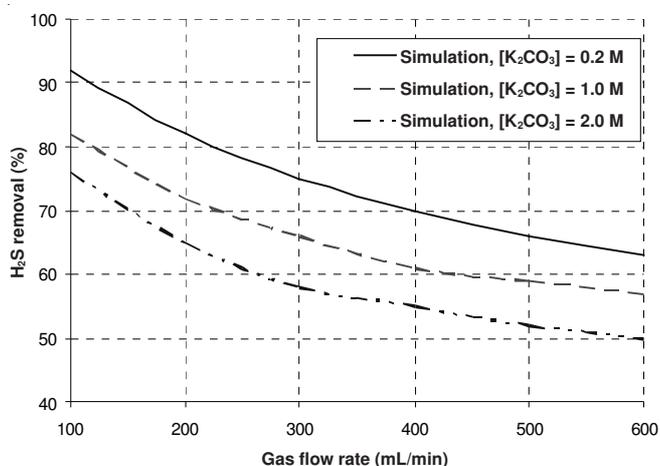


Fig. 2. Simulation results for different values of absorbent concentration as function of gas flow rate

The convective term in the shell has an opposite effect. Increasing liquid flow rate increases the removal rate (Fig. 3). As the solvent moves faster, the gas concentration at the outer

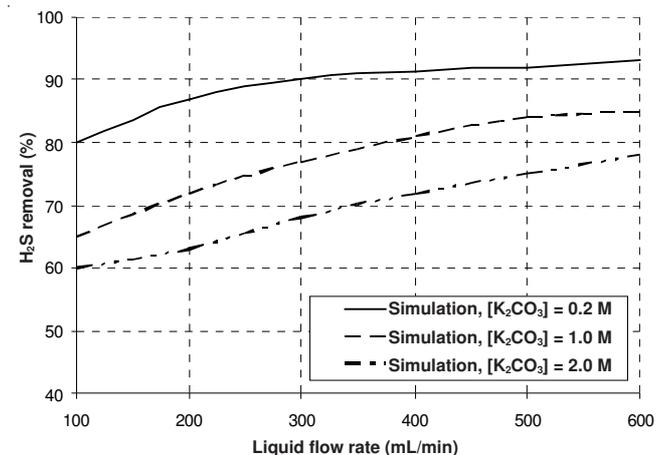


Fig. 3. Simulation results for different values of absorbent concentration as function of liquid flow

surface of the fiber along the length of the contactor becomes less, resulting in higher concentration gradient at the interface and thus higher H<sub>2</sub>S removal rate. Furthermore, the figures clearly shows that increasing of absorbent concentration from 0.2-2.0 M decreases the per cent H<sub>2</sub>S removal because the solubility of H<sub>2</sub>S in the solvent decreases from 2.31 to 0.39.

## Conclusion

In this work, the absorption of H<sub>2</sub>S in aqueous solution of potassium carbonate using a hollow-fiber membrane module was studied. A mathematical model was developed to describe absorption of H<sub>2</sub>S in the module. The hollow-fiber membrane module was found to be efficient in purification of gas streams containing soluble toxic gases. The simulation results for the absorption of H<sub>2</sub>S in liquid solvent indicated that the removal of H<sub>2</sub>S increased with increasing liquid velocity in the shell side.

## Nomenclature

A	: Cross section of tube (m <sup>2</sup> )
C	: Concentration (mol/m <sup>3</sup> )
D	: Diffusion coefficient (m <sup>2</sup> /s)
J <sub>i</sub>	: Diffusive flux of any species (mol/m <sup>2</sup> s)
k	: Reaction rate coefficient of H <sub>2</sub> S with absorbent (m <sup>3</sup> /mol s)
P	: Pressure (Pa)
T	: Temperature (K)
u	: Average velocity (m/s)
V	: Velocity in the module (m/s)
z	: Axial coordinate (m)

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